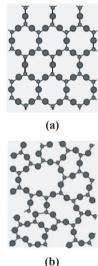
# **SOLID STATE**

#### 1. THE SOLID STATE:

The solid are characterised by incompressibility, rigidity and mechanical strength. The molecules, atoms or ions in solids are closely packed i.e. they are held together by strong forces and can not move about at random. Thus solids have definite volume, shape, slow diffusion, low vapour pressure and possesses the unique property of being rigid.

#### 2. AMORPHOUS AND CRYSTALLINE SOLIDS

Solids can be classified as *crystalline* or *amorphous* on the basis of the nature of order present in the arrangement of their constituent particles. A crystalline solid usually consists of a large number of small crystals, each of them having a definite characteristic geometrical shape. In a crystal, the arrangement of constituent particles (atoms, molecules or ions) is ordered. It has *long range order* which means that there is a regular pattern of arrangement of particles which repeats itself periodically over the entire crystal. Sodium chloride and quartz are typical examples of crystalline solids. An amorphous solid (Greek *amorphos* = no form) consists of particles of irregular shape. The arrangement of constituent particles (atoms, molecules or ions) in such a solid has only **short** Fig. 1.1: Two dimensional structure of range order. In such an arrangement, a regular and periodically repeating pattern is observed over short distances only.



(a) quartz and (b) quartz glass

Such portions are scattered and in between, the arrangement is disordered. The structures of quartz (crystalline) and quartz glass (amorphous) are shown in Fig. 1.1 (a) and (b) respectively. While the two structures are almost identical, yet in the case of amorphous quartz glass there is no long range order. The structure of amorphous solids is similar to that of liquids. Glass, rubber and plastics are typical examples of amorphous solids. Due to the differences in the arrangement of the constituent particles, the two types of solids differ in their properties.

JEE-Chemistry ALLEN

Crystalline solids have a sharp melting point. On the other hand, amorphous solids soften over a range of temperature and can be moulded and blown into various shapes. On heating they may become crystalline at some temperature. Some glass objects from ancient civilisations are found to become milky in appearance because of some crystallisation. Like liquids, amorphous solids have a tendency to flow, though very slowly. Therefore, sometimes these are called *pseudo solids* or *super cooled liquids*. Glass panes fixed to windows or doors of old buildings are invariably found to be slightly thicker at the bottom than at the top. This is because the glass flows down very slowly and makes the bottom portion slightly thicker.

Crystalline solids are *anisotropic* in nature, that is, some of their physical properties like electrical resistance or refractive index show different values when measured along different directions in the same crystals. This arises from different arrangement of particles in different directions. This is illustrated in Fig. 1.2. Since the arrangement of particles is different along different directions, the value of same physical property is found to be different along each direction. Amorphous solids on the other hand are *isotropic* in nature. It is because there is no *long range* order in them and arrangement is irregular along all the directions. Therefore, value of any physical property would be same along any direction. These differences are summarised in Table below:

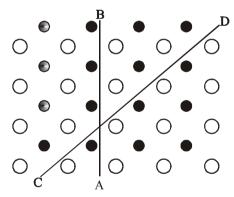


Fig. 1.2: Anisotropy in crystals is due to different arrangement of particles along different directions.



## Distinction between Crystalline and Amorphous Solids

Property	Crystalline Solids	Amorphous Solids
Shape	Definite characteristic geometrical shape	Irregular shape
Melting point	Melt at a sharp and characteristic	Gradually soften over a range of
	temperature	temperature
Cleavage	When cut with a sharp edged tool, they	When cut with a sharp edged tool, they
property	split into two pieces and the newly	cut into two pieces with irregular
	generated surfaces are plane and smooth	surfaces
Heat of fusion	They have a definite and characteristic	They do not have definite heat of fusion
	heat of fusion	
Anisotropy	Anisotropic in nature	Isotropic in nature
Nature	True solids	Pseudo solids or super cooled liquids
Order in	Long range order	Only short range order.
arrangement		
of constituent		
particles		

## Ex.1 Classify the following as amorphous or crystalline solids:

- (a) Polyurethane
- (b) Napthalene
- (c) Benzoic acid
- (d) Teflon
- (e) Potassium nitrate
- (f) Cellophane
- (g) Polyvinyl chloride
- (h) Fibre glass

(i) Copper

**Sol.** Crystalline: (b), (c), (e), (i)

Amorphous: (a), (d), (f), (g), (h)

**Note:** Polymeric substances are generally amorphous.

## 3. TYPES OF THE CRYSTALLINE SOLID

Tymes of Colid	Constituent	Bonding/	Examples	Physical	Electrical	Melting
Types of Solid	Particles	Attractive forces	Examples	Nature	Conductivity	Point
(1) Molecular Solids						
(i) Non polar	Molecules	Disppersion or	Ar, CCl <sub>4</sub> , H <sub>2</sub> , I <sub>2</sub>	Soft	Insulator	Very low
		London forces	$CO_2$			
(ii) Polar		Dipole-dipole	HCl, SO,	Soft	Insulator	Low
(iii) Hydrogen		Hydrogen	H <sub>2</sub> O (ice)	Hard	Insulator	Low
bonded		bonding	2 - ( )			
(2) Ionic Solids	Ions	Coulombic or	NaCl, MgO,	Hard but	Insulator in	High
		electrostatic	ZnS, CaF,	brittle	solid state but	
			Ziio, cui 2		conductors	
					in molten	
					state and in	
					aqueous	
					solutions	
(3) Metallic Solids	Positive ions	Metallic	Fe, Cu, Ag, Mg	Hard but	Conductors in	Fairly
	in a sea of	bonding	, , , , , , , , , ,	malleable	solid state as	high
	delocalised			and	well as in	
	electrons			ductile	molten state	
(4) Covalent or	Atoms	Covalent	SiO <sub>2</sub> (quartz)	Hard	Insulators	Very
network Solids		bonding	SiC,			high
			C (diomond)			
			AIN,			
			C(graphite)	Soft	Conductor	

# Ex.2 Classify the following solids in different categories based on the nature of intermolecular forces operating in them:

(a)	Potassium sulphate $(K_2SO_4)$	<b>(b)</b>	Tin (Sn)
(c)	Benzene (C <sub>6</sub> H <sub>6</sub> )	<b>(d)</b>	Urea (NH <sub>2</sub> CONH <sub>2</sub> )
(e)	Ammonia (NH <sub>3</sub> )	<b>(f)</b>	Water (H <sub>2</sub> O)
<b>(g)</b>	Zinc sulphide (ZnS)	(h)	Graphite (C)
(i)	Rubidium (Rb)	<b>(j</b> )	Argon (Ar)
( <b>k</b> )	Silicon carbide (SiC)	(l)	Bronze



**Sol.** Ionic solids: (a), (g)

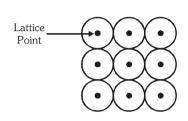
Metallic solids: (b), (i), (l)

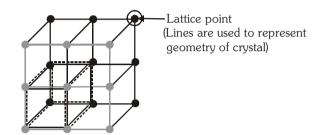
Molecular solids: (c), (d), (e), (f), (j)

Covalent network solids.: (h), (k)

#### 4.0 SOME BASIC DEFINITION:

#### 4.1 SPACE LATTICE (CRYSTAL LATTICE:





The main characteristic of crystalline solids is a regular and repeating pattern of constituent particles. If the three dimensional arrangement of constituent particles in a crystal is represented diagrammatically, in which each particle is depicted as a point, the arrangement is called crystal lattice. Thus, *a regular three dimensional arrangement of points in space is called a crystal lattice*. A portion of a crystal lattice is shown in Fig. The following are the characteristics of a crystal lattice:

- (a) Each point in a lattice is called *lattice point* or *lattice site*.
- (b) Each point in a crystal lattice represents one constituent particle which may be an atom, a molecule (group of atoms) or an ion.
- (c) Lattice points are joined by straight lines to bring out the geometry of the lattice.

#### 4.2. UNIT CELL:

Unit cell is the smallest portion of a crystal lattice which, when repeated in different directions, generates the entire lattice.

A unit cell is characterized by the edge lengths a, b and c along the three edges of the unit cell and the angles  $\alpha$ ,  $\beta$  and  $\gamma$  between the pair of edges : bc, ca and ab, respectively.

#### TYPE OF UNIT CELLS -

#### 4.2.1 Primitive and Centred Unit cells

Unit cells can be broadly divided into two categories, primitive and centred unit cells.

- (a) Primitive Unit Cells (P)
  - When constituent particles are present only on the corner positions of a unit cell, it is called as **primitive unit cell.**
- **(b)** Centred Unit Cells: When a unit cell contains one or more constituent particles present at positions other than corners in addition to those at corners, it is called a centred unit cell. Centred unit cells are of three types:
- (i) **Body-Centred Unit Cells (I):** Such a unit cell contains one constituent particle (atom, molecule or ion) at its body-centre besides the ones that are at its corners.
- (ii) **Face-Centred Unit Cells (F):** Such a unit cell contains one constituent particle present at the centre of each face, besides the ones that are at its corners.
- (iii) **End-Centred Unit Cells (E):** In such a unit cell, one constituent particle is present at the centre of any two opposite faces besides the ones present at its corners.

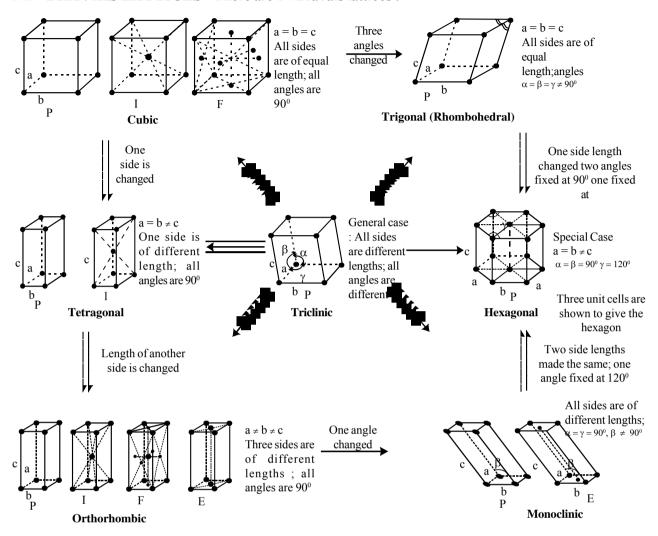
#### 4.3. THE SEVEN CRYSTAL SYSTEMS

On the basis of the classification of symmetry, the lattice have been divided into seven systems. These can be grouped into 7 crystal systems. These seven systems with the characteristics of their axes (angles and intercepts) along with some examples of each are given in the following table:

Seven Primitive Unit cells and their Possible Variations as Centred Unit Cells

Crystal system	Possible Variations	Axial distance or edge lengths	Axial angles	Examples
Cubic	Primitive, body-centred,	a = b = c	$\alpha = \beta = \gamma = 90^{\circ}$	NaCl, Zinc blende, Cu
	Face centre			
Tetragonal	Primitive, Body-centred	$a = b \neq c$	$\alpha = \beta = \gamma = 90^{\circ}$	White tin, SnO <sub>2</sub> , TiO <sub>2</sub> , CaSO <sub>4</sub>
Orthorhombic	Primitive, Body-centred,	a ≠ b ≠ c	$\alpha = \beta = \gamma = 90^{\circ}$	Rhombic sulphur,
	Face-centred, End-centred			KNO <sub>3</sub> , BaSO <sub>4</sub>
Hexagonal	Primitive	$a = b \neq c$	$\alpha = \beta = 90^{\circ}$ , $\gamma = 120^{\circ}$	Graphite, ZnO, CdS,
Rhombohedral or	Primitive	a = b = c	$\alpha = \beta = \gamma \neq 90^{\circ}$	Calcite (CaCO <sub>3</sub> ),
Trigonal			, .	HgS (Cinnabar)
Monoclinic	Primitive, End-centred	a ≠ b ≠ c	$\alpha = \gamma = 90^{\circ}, \beta \neq 90^{\circ}$	Monoclinic sulphur,Na <sub>2</sub> SO <sub>4</sub> ·10H <sub>2</sub> O
Triclinic	Primitive	a ≠ b ≠ c	$\alpha \neq \beta \neq \gamma \neq 90^{\circ}$	K <sub>2</sub> Cr <sub>2</sub> O <sub>7</sub> ,CuSO <sub>4</sub> .5H <sub>2</sub> O,H <sub>3</sub> BO <sub>3</sub>

#### **4.4. BRAVAIS LATTICES**: There are 14 Bravais lattices:



#### **4.5. CO-ORDINATION NUMBER:**

The number of nearest particles around a specific particle in a given crystalline substance is called *co-ordination* number.



#### PACKING EFFICIENCY OR PACKING DENSITY (P.E.): 4.6.

Packing efficiency is defined as the ratio of volume occupied by the constituent particles to the total volume of the crystalline substance.

$$P.E. = \frac{Volume \ occupied \ by \ particles \ present \ in a \ crystal}{Volume \ of \ crystal}$$

P.E. 
$$=\frac{Z\times(4/3)\pi r^3}{V}$$
, where  $Z=$  number of atoms present in unit cell

#### DENSITY OF THE CRYSTAL:

$$Density of crystal = Density of an unit cell = \frac{Mass of unit cell}{Volume of unit cell} \\ Mass of the unit cell = Number of particles present in a unit cell \times Mass of one particles = Z \times m$$

But mass of one particles (m) = 
$$\frac{\text{Particle mass}}{\text{Avogadro Number}} = \frac{M}{N_A}$$

Mass of an unit cell = 
$$Z \times \frac{M}{N_A}$$
  
Density of an unit cell =  $\frac{Z \times \frac{M}{N_A}}{V}$ 

Density of an unit cell = 
$$\frac{Z \times \frac{N}{N_A}}{V}$$

... Density of Crystal, 
$$d = Density of an unit cell = \frac{Z \times M}{V \times N_A} g \text{ cm}^{-3}$$

#### **ANALYSIS OF CUBIC CRYSTAL:** 5.0

#### **5.1. GEOMETRY OF A CUBE**

Number of corners = 8

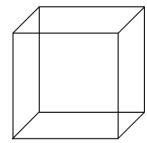
Number of faces = 6

Number of edges = 12

Number of cube centre = 1

Number of cube diagonals = 4

Number of face diagonals = 12



Space for Notes

# 5.2 CONTRIBUTION OF A CONSTITUENT PARTICLE AT DIFFERENT SITES OF CUBE:

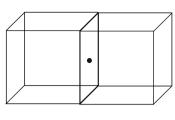
**5.2.1** A corner of a cube is common in 8 cubes.

So  $\frac{1}{8}$  th part of a particle is present at this corner of cube.



**5.2.2** A face of a cube is common is 2 cubes.

So  $\frac{1}{2}$  th part of a particle is present at the face of a cube.



**5.2.3** An edge of a cube is common in four cubes,

so  $\frac{1}{4}$ th part of particle is present at the edge of a cube

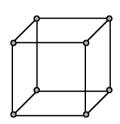


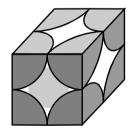
#### **5.3** TYPE OF CUBIC UNIT CELL:

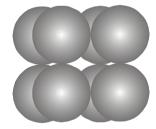
#### 5.3.1 Simple/Primitive/Basic Unit cell (Simple cubic, SC);

A unit cell having lattice point only at corners called as primitive or simple unit cell. In this case there is one particle at each of the eight corners of the unit cell.

Considering a particles at one corner as the centre, it will be found that this atom is surrounded by six equidistant neighbours (particles) and thus the co-ordination number will be six. If 'a' is the side of the unit cell, then the distance between the nearest neighbours shall be equal to 'a'.

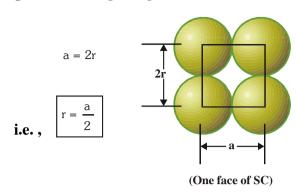






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# (a) Relationship between Edge length 'a' and Particle radius 'r':-



- (b) Number of particles present in unit cell (Z): In this case one particle lies at each corner. Hence simple cubic unit cell contains a total of  $\frac{1}{8} \times 8 = 1$  particle/unit cell.
- (c) Packing efficiency (P. E.):

P.E. = 
$$\frac{\text{Volume occupied by particles present in unit cell}}{\text{Volume of unit cell}} = \frac{Z \times \frac{4}{3} \pi r^3}{V}$$
 [ Volume of atom =  $\frac{4}{3} \pi r^3$ ]

$$P.E. = \frac{1 \times \frac{4}{3} \times \pi \times \left(\frac{a}{2}\right)^{3}}{a^{3}} = \frac{\pi}{6} = 0.52 \text{ or } 52\%$$
 [  $r = \frac{a}{2}$  and  $V = a^{3}$ ,  $Z = 1$ ]

In SC, 52% of total volume is occupied by particles.

- :. Void space  $\approx (100 52) = 48 \%$
- (d) Coordination number (CN)

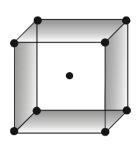
Nearestneighbour	Distance	Number
1	a	6
2	$\sqrt{2}$ a	12
3	$\sqrt{3}$ a	8

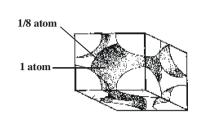
Space for Notes

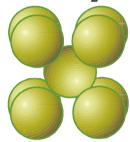


## 5.3.2. Body Centred Cubic unit cell (BCC):

A unit cell having lattice point at the body centre in addition to the lattice points at every corner is called as body centered unit cell. Here the central particle is surrounded by eight equidistant particles and hence the co-ordination number is eight. The nearest distance between two particles will be  $\frac{a\sqrt{3}}{2}$ 





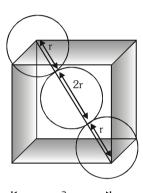


(a) Relationship between edge length 'a' and particle radius 'r':

In BCC, along cube diagonal all particles touches each other and the length of cube diagonal is  $\sqrt{3}a$ .

So, 
$$\sqrt{3}a = 4r$$

i.e. 
$$r = \frac{\sqrt{3}a}{4}$$



(b) Number of particle present in unit cell (Z):

$$Z = \left(\frac{1}{8} \times 8\right)$$
 +  $(1 \times 1) = 1 + 1 = 2$  particles/unit cell.

In this case one particle lies at the each corner of the cube. Thus contribution of the 8 corners is  $\left(\frac{1}{8} \times 8\right) = 1$ , while that of the body centred is 1 in the unit cell. Hence total number of particles per unit cell is 1 + 1 = 2

## Space for Notes

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# (c) Packing efficiency:

P.E. = 
$$\frac{Z \times \frac{4}{3} \pi r^3}{V} = \frac{2 \times \frac{4}{3} \times \pi \left(\frac{\sqrt{3}a}{4}\right)^3}{a^3} = \frac{\sqrt{3}\pi}{8} = 0.68 \text{ or } 68\%$$
 [  $Z = 2, r = \frac{\sqrt{3}a}{4}, V = a^3$ ]

In BCC, 68% of total volume is occupied by particles.

:. Void space = 
$$100 - 68 = 32 \%$$

### (d) Coordination number (CN)

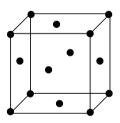
Nearest neighbour	Distance	Number
1	$\sqrt{3}\frac{a}{2}$	8
2	a	6
3	$\sqrt{2}$ a	12

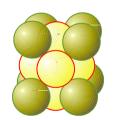
#### 5.3.3 Face Centred Cubic unit cell (FCC):

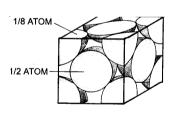
A unit cell having lattice point at every face centre in addition to the lattice point at every corner called as face centred unit cell.

In this case there are eight particles at the eight corners of the unit cell and six particles at the centre of six faces. Considering a particle at the face centre as origin, it will be found that this face is common to two cubes and there are twelve points surrounding it situated at a distance which is equal to half the face diagonal of the unit cell. Thus the co-ordination number will be twelve and the distance between the two

nearest particles will be  $\frac{a}{\sqrt{2}}$ .







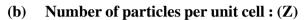
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#### Relationship between edge length 'a' and atomic radius 'r': (a)

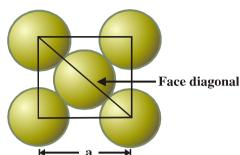
In FCC, along the face diagonal all atoms touches each other and the length of face diagonal is  $\sqrt{2}a$ .

So 
$$4r = \sqrt{2}a$$

i.e. 
$$r = \frac{a}{2\sqrt{2}}$$



$$Z = \left(\frac{1}{8} \times 8\right) + \left(6 \times \frac{1}{2}\right) = 1 + 3 = 4 \text{ particles/unit cell}$$
Corner faces



In this case, one particle lies at the each corner of the cube and one particle lies at the centre of each face of the cube. It may noted that only 1/2 of each face sphere lie within the unit cell and there are six such faces. The total contribution of 8 corners is  $\left(\frac{1}{8} \times 8\right) = 1$ , while that of 6 face centred particles is  $\left(\frac{1}{2} \times 6\right) = 3$  in the unit cell.

Hence, total number of particles per unit cell is 1 + 3 = 4

#### (c) **Packing efficiency:**

P.E. = 
$$\frac{Z \times \frac{4}{3} \pi r^3}{V}$$
 [Z = 4, r =  $\frac{a}{2\sqrt{2}}$ , V = a<sup>3</sup>]  
=  $\frac{4 \times \frac{4}{3} \pi \times \left(\frac{a}{2\sqrt{2}}\right)^3}{a^3} = \frac{\pi}{3\sqrt{2}} = 0.74 \text{ or } 74\%$ 

In FCC, 74% of total volume is occupied by particles. This is maximum for crystals having identical particles.

$$\therefore \text{ Void space} = 100 - 74 = 26 \%$$
**Space for Notes**

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## (d) Coordination number (CN)

Nearestneighbour	Distance	Number
1	$\frac{a}{\sqrt{2}}$	12
2	a	6
3	$\sqrt{\frac{3}{2}}$ a	24

#### 5.4 SUMMARY OF CUBIC CRYSTAL:

Unit cell	No. of particles per unit cell(Z)	2r =	CN	Volume occupied by particles (%)
Simple cube(SC)	1	a	6	52
Body centred cube(BCC)	2	$\frac{a\sqrt{3}}{2}$	8	68
Facecentred cube(FCC)	4	$\frac{a}{\sqrt{2}}$	12	74

### **CLASS ILLUSTRATION - 01**

- 1. A solid crystallises in cubic crystal in which 'X' atoms occupy all the corners and body centres and 'Y' atoms occupy all the face-centres. What is the simplest formula of solid?
- 2. A metal has bcc structure and the edge length of its unit cell is 3.04 Å. The volume of the unit cell in  $cm^3$  will be
- 3. The density of Al is  $5.4 \text{ g/cm}^3$ . If it crystallise in fcc lattice, determine its atomic radius.
- 4. An element (atomic mass = 60) having face centred cubic crystal has a density of 6.23 g cm<sup>-3</sup>. What is the edge length of the unit cell? (Avogadro constant,  $N_A = 6.02 \times 10^{23} \text{ mol}^{-1}$ )



- 5. An element (molar mass = 60 gm/mole) crystallises in CCP lattice. If density is 6.25 gm/cm<sup>3</sup> and the distance between next nearest neighbour is  $d\mathring{A}$ , then the value of 'd' is  $(N_A = 6 \times 10^{23})$ .
- 6. Potassium crystallizes in a body-centred cubic lattice with edge length, a = 5.2 Å.
  - (a) What is the distance between nearest neighbours?
  - (b) What is the distance between next-nearest neighbours?
  - (c) How many nearest neighbours does each K atom have?
  - (d) How many next-nearest neighbours does each K atom have?
  - (e) What is the density of crystalline potassium?

(Given: 
$$K = 39$$
,  $(5.2)^3 = 140$ )

- 7. An element crystallizes in a structure having FCC unit cell of an edge 200 pm. Calculate the density, if 200 g of this element contains  $2.4 \times 10^{24}$  atoms.  $(N_A = 6 \times 10^{23})$
- 8. Iron crystallizes in several modifications. At about 910°C, the body-centred cubic ' $\alpha$ ' form undergoes a transition to the face-centred cubic ' $\gamma$ ' form. Assuming that the distance between nearest neighbours is the same in the two forms at the transition temperature, the ratio of the density of  $\gamma$  iron to that of  $\alpha$  iron at the transition temperature, x:1, then the value of  $(3\sqrt{6}x)$  is.
- 9. An element crystallizes into a structure which may be described by a cubic type of unit cell having one atom on each corner of the cube and two extra atoms on one of its body diagonal. If the volume of this unit cell is 2.4×10<sup>-23</sup> cm<sup>3</sup> and density of element is 7.2 g cm<sup>-3</sup>, calculate the number of atoms present in 288 g of element.

#### 6. CLOSE PACKING OF IDENTICAL SOLID SPHERES

The solids which have non-directional bonding, their structures are determined on the basis of geometrical consideration. For such solids, it is found that the lowest energy structure is that in which each particle is surrounded by the greatest possible number of neighbours. In order to understand the structure of such solids, let us consider the particles as hard sphere of equal size in three directions. Although there are many ways to arrange the hard spheres but the one in which maximum available space is occupied will be economical which is known as **closed packing**.

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To clearly understand the packing of these spheres, the packing can be categorised as:

- (i) Close packing in one dimension.
- (ii) Close packing in two dimension.
- (iii) Close packing in three dimension.

#### 6.1 CLOSE PACKING IN ONE DIMENSION:

In one dimension, only one arrangement of spheres is possible as shown in fig.



Close packing of spheres in one dimension

Each sphere is touched by other two spheres, hence coordination numbers of packing is two.

# 6.2 CLOSE PACKING IN TWO DIMENSION:

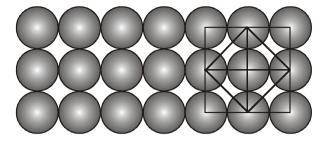
Two possible types of two dimensional packing are

- (i) Square close packing in two dimension.
- (ii) Hexagonal close packing in two dimension.

#### (i) Square close packing in two dimension:

When two rows are placed in such a manner, that spheres of one row are placed immediately below of the other, the resulting packing is called two dimensional square close packing.

- (i) Since all the rows are identical, the packing is called AAA ...... type packing.
- (ii) Each sphere is touched by four other, hence coordination number is four.
- (iii) If centres of spheres are connected, square cells are formed, hence it also called two dimensional square packing.
- (iv) This type of packing is not very effective in terms of utilisation of space.
- (v) Packing efficiency in 2-D =  $\frac{1 \times \pi r^2}{a^2} = \frac{1 \times \pi (a/2)^2}{a^2} = \frac{\pi}{4} = 0.78$  or 78%
- (vi) Packing efficiency in 3-D =  $\frac{1 \times \frac{4}{3} \pi \left(\frac{a}{2}\right)^3}{a^3} = 0.52$  or 52% [In 3-D, its unit cell is simple cubic]



#### (ii) Hexagonal close packing in two dimension:

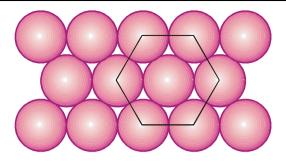
If various one dimensional close pack rows are placed in such a way that spheres of top row fits in depression of bottom row spheres, the resulting packing is called two dimensional hexagonal close packing.

- (i) Every third row sphere comes exactly at top of first row sphere, hence the packing is called ABABAB ..... packing.
- (ii) If centres are joined, hexagonal unit cells are formed. Hence this is called two dimensional hexagonal close packing.
- (iii) This packing is most efficient in utilising space in two dimensional arrangement.
- (iv) Each sphere is touched by six other, hence coordination number is six.

(v) Packing efficiency in 2-D = 
$$\frac{3 \times \pi \left(\frac{a}{2}\right)^2}{\frac{a^2 \sqrt{3}}{4} \times 6} = \frac{\pi}{2\sqrt{3}} = 0.90 \text{ or } 90\%$$

(vi) Packing efficiency in 3-D =  $\frac{3 \times \frac{4}{3} \pi \left(\frac{a}{2}\right)^3}{\frac{a^2 \sqrt{3}}{4} \times 6 \times a} = \frac{\pi}{3\sqrt{3}} = 0.60 \text{ or } 60\%$ 





#### 6.3 CLOSE PACKING IN THREE DIMENSIONS:

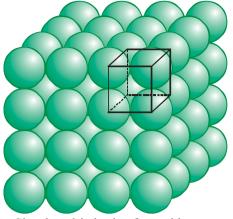
When two dimensional packing structure are arranged one above the other, depending upon type of two dimensional arrangement in a layer, and the relative positions of spheres in above or below layer, various types of three dimensional packing results. To define 3-D lattice, six lattice parameters are required - 3 edge lengths & 3 angles.

- (i) Simple cubic packing (AAAA.....)
- (ii) Hexagonal close packing (ABABAB.....)
- (iii) Cubic close packing or face centred cubic (ABC ABC...)

# **6.3.1** Three dimensional close packing from square two dimensional packing (Simple cubic packing in three dimension)

The two dimensional square close packed layer are placed, in such a manner that spheres in each layer comes immediately on top of below layer, simple cubic packing results. Important points:

- (i) Spheres all aligned vertically and horizontally in all directions.
- (ii) The unit cell for this packing is simple cubic unit cell.
- (iii) In this packing, only 52% of available space is occupied by spheres.
- (iv) Each sphere is in contact will six spheres and hence coordination number is 6.
- (v) Packing efficiency =  $\frac{1 \times \frac{4}{3} \pi r^3}{(2r)^3} = \frac{\pi}{6} \approx 0.52$



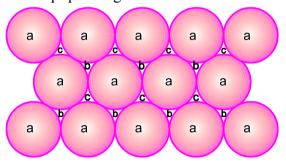
First neighbour = 6 at a distance = a Second neighbour = 12 at  $(\sqrt{2}a)$  distance Third neighbour = 8 at  $(\sqrt{3}a)$  distance

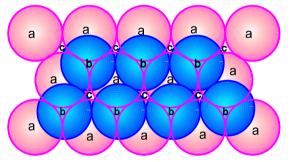
Coordination number = 6

Simple cubic lattice formed by A A A ... arrangement

#### 6.3.2 Three dimensional close packing from hexagonal two dimensional packing:

In hexagonal close packing, there are two types of the voids (open space or space left) which are divided into two sets 'b' and 'c' for convenience. The spaces marked 'c' are curved triangular spaces with tips pointing upwards whereas spaces marked 'b' are curved triangular spaces with tips pointing downwards.





Now we extend the arrangement of spheres in three dimensions by placing second close packed layer (hexagonal close packing) (B) on the first layer (A). The spheres of second layer may placed either on space denoted by 'b' or 'c'. It may be noted that it is not possible to place spheres on both types of voids (i.e. b and c). Thus half of the voids remain unoccupied by the second layer. The second layer also have voids of the types 'b' and in order to build up the third layer, there are following ways:

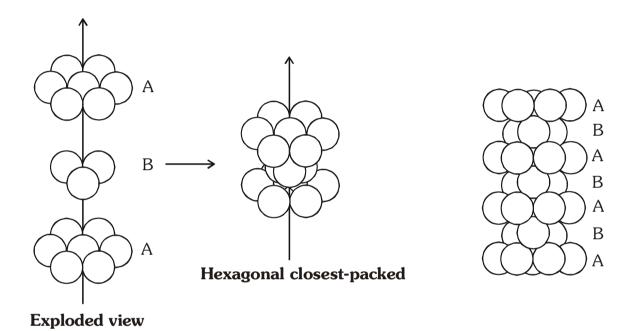
**Space for Notes** 

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## (I) Hexagonal close packing (HCP)

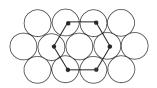
(i) In one way, the spheres of the third layer lie on the spaces of second layer (B) in such a way that they lie directly above those in the first layer(A). In other words we can say that the third layer becomes indentical to the first layer. Such arrangement is called AB AB AB ....type packing or hexagonal close packing (hcp).

- (ii) Maximum possible space is occupied by spheres.
- (iii) Each sphere is touched by 12 other spheres in 3D (6 is one layer, 3 in top layer and 3 in bottom) and hence the coordination number is 12.



# Packing efficiency of HCP units Relation between a, b, c and R:

$$a = b = 2R$$



$$\tan 30^{\circ} = \frac{a}{2 \times y}$$

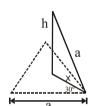
So 
$$y = \frac{a \times \sqrt{3}}{2 \times 1} = \frac{\sqrt{3}}{2} a.$$

Base Area = 
$$6\left[\frac{1}{2} \times \frac{\sqrt{3}}{2}\right] = \frac{6\sqrt{3}a^2}{4}$$

#### Calculation of c:

$$\cos 30^{\circ} = \frac{a}{2 \times x}$$

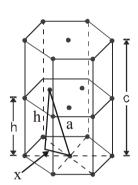
$$\cos 30^{\circ} = \frac{a}{2 \times x} \qquad \qquad x = \frac{2a}{2 \times \sqrt{3}} = \frac{a}{\sqrt{3}}$$



Applying pythogoras theorem :  $x^2 + h^2 = a^2$ 

So 
$$h^2 = a^2 - x^2 = a^2 - \frac{a^2}{3} = \frac{2}{3}a^2$$

$$h = \sqrt{\frac{2}{3}} a$$
 so  $c = 2h = 2\sqrt{\frac{2}{3}} a$ 



So volume of hexagon = area of base  $\times$  height

$$= \frac{6.\sqrt{3}}{4} \times a^2 \times 2\sqrt{\frac{2}{3}} a = \frac{6.\sqrt{3}}{4} \times (2R)^2 + 2\sqrt{\frac{2}{3}} \times (2R) = 24\sqrt{2} R^3$$

#### Space for Notes

## (v) Effective no. of particles (Z)

$$Z = 3 + 2 \times \frac{1}{2} + 12 \times \frac{1}{6} = 3 + 1 + 2 = 6.$$

It must be noted that all three spheres of 'B' layer are not exactly inside the unit cell. But the contribution of three spheres are taken because the same volume of other spheres in that layer is also inside the unit cell.

(vi) Packing efficiency = 
$$\frac{6 \times \frac{4}{3} \pi}{24 \sqrt{2} R^3} = \frac{\pi}{3\sqrt{2}} = 0.74 \text{ or } 74\%.$$

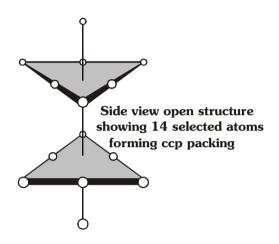
(vii) Density (d) = 
$$\frac{\text{mass}}{\text{volume}} = \left[\frac{Z \times M}{N_A \times \text{volume}}\right]$$

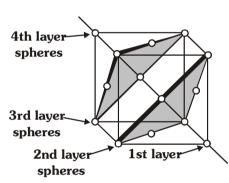
### (II) Cubic close packing (CCP) or face centered cubic (FCC)

In second way, the spheres of the third layer (C) lie on the second layer (B) in such a way that they lie over the unoccupied spaces 'C' of the first layer(A). If this arrangement is continued in the same order every fourth layer becomes identical to the first. Such arrangement of particle is called ABC ABC ABC.... or cubic close packing (ccp) or face centered cubic (fcc).

It may be noted that in ccp (or fcc) structures, each sphere is surrounded by 12 spheres hence the coordination number of each sphere is 12. The spheres occupy 74% of the total volume and 26% of is the empty space in both (hcp and ccp) structures.

Side view exploded space filling diagram showing 14 selected atom forming ccp packing





fcc unit cell showing 14 spheres

(i) Relation between 'a' and 'R':

 $a \neq 2R$ 

 $\sqrt{2}a = 4R$  (sphere are touching along the face diagonal)

(ii) Effective no. of particles per unit cell (Z)

$$Z = \frac{1}{8} \times 8 + \frac{1}{2} \times 6 = 4$$

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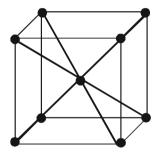
# (iii) Packing fraction:

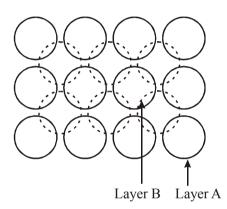
P.F. = 
$$\frac{4 \times \frac{4}{3} \pi}{4 \times 4 \times 4} \frac{R^3}{R^3} \times \sqrt{2} \times 2 = \frac{\pi}{3\sqrt{2}} = 0.74 \text{ or } 74\%$$

(iv) Density (d) = 
$$\frac{Z \times M}{N_A \times a^3}$$

#### 6.3.3 Body centred cubic (bcc):

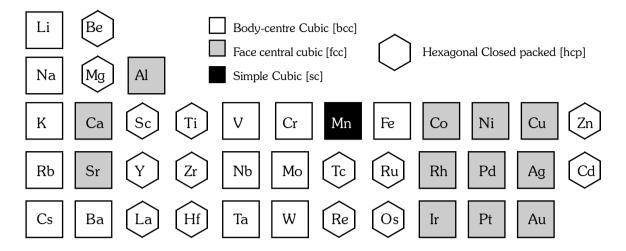
There is another possible arrangement of packing of spheres known as body centred cubic (bcc) arrangement. This arrangement is observed in square close packing in which there is suitable space between the spheres in each layer. In bcc arrangement, the spheres of the second layer lie at the space (hollows or voids) in the first layer.





Thus each sphere of the second layer touches four spheres of the first layer. Now spheres of the third layer are placed exactly about the spheres of first layer. In this way each sphere of the second layer touches eight spheres (four of 1st layer and four of IIIrd layer). Therefore coordination number of each sphere is 8 in bcc sturcture. The spheres occupy 68% of the total volume 32% of the volume is the empty space.

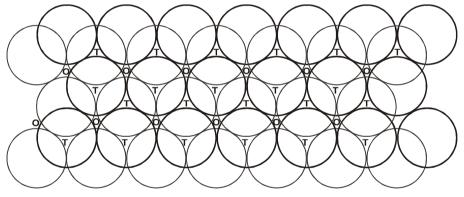
#### 7. STRUCTURES OF VARIOUS ELEMENTS



#### 8. INTERSTICES OR VOIDS OR HOLES IN CRYSTALS

It has been shown that the particles are closely packed in the crystals even than there is some empty space left in between the spheres. This is known as interstices (or interstitial site or hole or empty space or voids). In three dimentional close packing (CCP & HCP) the interstices are of two types:

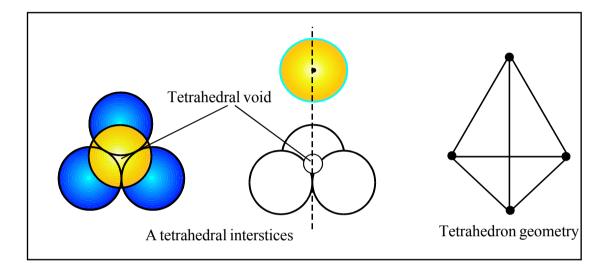
(i) tetrahedral voids and (ii) octahedral voids.



A stack of two layers of close packed spheres and voids generated in them. T = Tetrahedral void; O = Octahedral void

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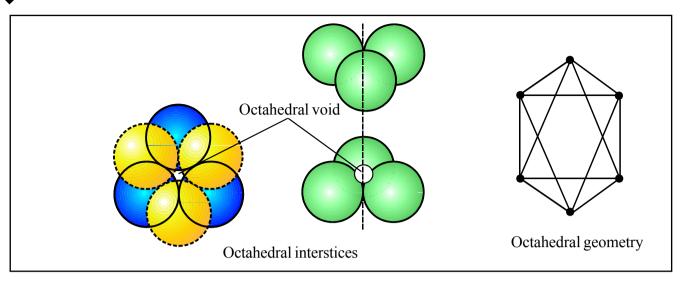
(i) Tetrahedral voids: We have seen that in hexagonal close packing (hcp) and cubic close packing (ccp), each sphere of second layer touches with three spheres of first layer. Thus, they leave a small space in between which is known as **tetrahedral site or interstices**. In another words, the vacant space between 4 touching spheres is called as tetrahedral void. Since a sphere touches three spheres in the below layer and three spheres in the above layer hence there are two tetrahedral sites associated with one sphere. It may by noted that a tetrahedral site does not mean that the site is tetrahedral in geometry but it means that this site is surrounded by four spheres and the centres of these four spheres lie at the apices of a regular tetrahedron.



- (ii) Octahedral voids: Hexagonal close packing (hcp) and cubic close packing (ccp) also form another type of interstices (or site), which is called octahedral site (or interstices). In another words, the vacant space between 6 touching spheres is called as octahedral void.
  - In the figure two layers of close packed spheres are shown. The spheres of first layer are shown by full circles while that of second layer by dotted circles. Two triangles are drawn by joining the centres of three touching spheres of both the layers.

Space for Notes

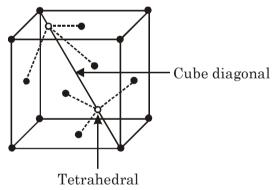




The apices of these triangles point are in opposite directions. On super imposing these triangles on one another, an octahedral site is created. It may be noted that an octahedral site does not mean that the hole is octahedral in shape but it means that this site is surrounded by six nearest neighbour lattice points arranged octahedrally.

#### 8.1 POSITIONS OF TETRAHEDRAL VOIDS IN AN FCC UNIT CELL:

In FCC, one corner and its three face centred atom of faces meeting at that corner form a tetrahedral void. In FCC, two tetrahedral voids are obtained along one cube diagonal. So in FCC 8 tetrahedral voids are present.



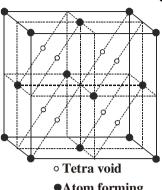
**Space for Notes** 

Alternatively, the centre of tetrahedral void is located on the centre of body diagonal of each small cube of volume  $\left(\frac{a^3}{8}\right)$ .

Total number of particles per unit cell =  $\frac{1}{2} \times 6 + 8 \times \frac{1}{8} = 4$ 

Total number of tetrahedral void = 8

Effective number of tetrahedral void per particle = 2.



Atom forming fcc packing

#### 8.2 POSITION OF OCTAHEDRAL VOID IN FCC UNIT CELL:

Position of octahedral void is at mid-point of each edge (total 12 edges in a cube) and at the centre of cube.

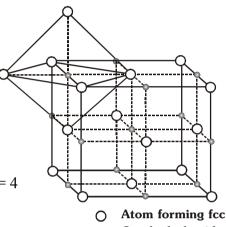
Each octahedral void located at mid point of edge contributes 1/4 to the unit cell. The octahedral void situated at the centre contributes 1.

In FCC, total number of octahedral voids are

$$(1 \times 1)$$
 +  $(12 \times \frac{1}{4}) = 1 + 3 = 4$   
(Cube centre) (edge)

In FCC, number of particles = 4

Effective number of octahedral voids per particle = 1 *:* .



Octahedral void

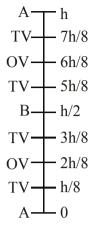
#### 8.3 POSITION OF TETRAHEDRAL AND OCTAHEDRAL VOID IN HCP:

- Above & below each sphere, there is a tetrahedral void, hence number of tetrahedral void per (i) unit cell = 12
- Other than TV, all voids are OV & number of OV per unit cell =  $2 \times 3 = 6$ (ii)

# Space for Notes



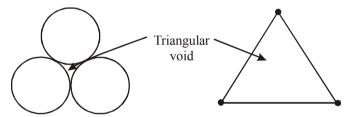
## **Height of voids from Base:**



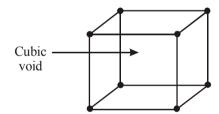
Note: In any closed packing of maximum efficiency, there are two TV & one OV per particle

### 8.4 Triangular and cubic voids:

(i) **Triangular void :** It is formed by three spheres in a plane.



(ii) Cubic void: It is formed in simple cubic unit cell by eight spheres at the corners of cube.



**Space for Notes** 

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# 9. CRYSTAL OF DIAMOND

The crystal is FCC for C atom & alternate tetrahedral voids are also occupied by carbon atoms.

\* 
$$Z = \frac{1}{8} \times 8 + 6 \times \frac{1}{2} + 4 = 8$$

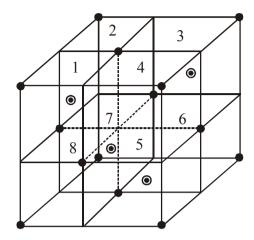
\* 
$$CN = 4$$

\* 
$$\frac{\sqrt{3}a}{4} = 2r = d_{C-C}$$

\* Number of C–C bonds/unit cell = 
$$4 \times 4 = 16$$

\* Number of C–C bonds/C-atom = 
$$\frac{16}{8}$$
 = 2

\* PE = 
$$\frac{8 \times \frac{4}{3} \pi r^2}{\left(\frac{8r}{\sqrt{3}}\right)^3} = \frac{\sqrt{3}\pi}{16} \approx 0.34 \text{ or } 34\%$$



# 10 PACKING IN IONIC SOLID

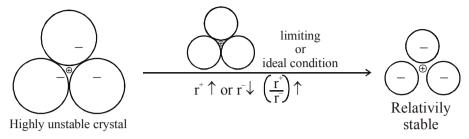
- (i) Normally anions are bigger than cations, hence ionic solid are considered as the packing of anions and cations are supposed to occupy the voids.
- (ii) Oppositively charged particles should lie closer and smilarly charged particles should lie away from each other.
- $\textbf{(iii)} \quad \text{Each ion tend to maximise its coordination number (Number of oppositively charged ions around it)}.$

Point (ii) and (iii) contradict each other because on increase the CN, the repulsion between like charges will also increases. Hence, in all the ionic solids, there must be a balance with the help of relative size of ions to ensure maximum CN and minimum repulsion between like charges.

Space for Notes



# 10.1 LIMITING OR IDEAL RADIUS RATION $\left(\frac{r^+}{r^-}\right)$ :



The minimum  $\frac{r^+}{r^-}$  values for the existence of a cation in a particular void is called **limiting radius** ratio for that void.

With the increase in radius ratio, space between anion will increase & hence the cation may tend for higher coordination number.

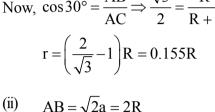
Voids	CN	Limiting r <sup>+</sup> /r <sup>-</sup>	Range of r <sup>+</sup> /r <sup>-</sup>
Triangular	3	0.155	0.155 - 0.225
Tetrahedral	4	0.225	0.225 - 0.414
Octahedral	6	0.414	0.414 - 0.732
Cubic	8	0.732	0.732 - 1.000

<sup>\*</sup> For values lesser than 0.155, crystal will not exist.

Ex.3 Calculate the radius (r) of largest sphere which may be fitted in the (i) triangular voids (ii) tetrahedral voids (iii) octahedral voids (iv) cubic voids made by identical spheres of radius, 'R', without disturbing the crystal.

Sol. (i) 
$$AB = R$$
  
 $AC = R + r$   
 $\angle BAC = 30^{\circ}$ 

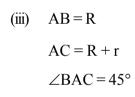
Now, 
$$\cos 30^\circ = \frac{AB}{AC} \Rightarrow \frac{\sqrt{3}}{2} = \frac{R}{R+r}$$
  
$$r = \left(\frac{2}{\sqrt{3}} - 1\right)R = 0.155R$$



(II) 
$$AB = \sqrt{2}a = 2R$$

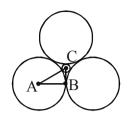
$$AC = \frac{\sqrt{3}a}{2} = R + r$$
Now, 
$$\frac{R+r}{R} = \frac{\sqrt{3}}{\sqrt{2}}$$

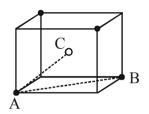
$$\therefore \qquad r = \left(\sqrt{\frac{3}{2}} - 1\right)R = 0.225R$$



Now, 
$$\cos 45^\circ = \frac{AB}{AC} \Rightarrow \frac{1}{\sqrt{2}} = \frac{R}{R+r}$$

$$\therefore \qquad r = \left(\sqrt{2} - 1\right)R = 0.414R$$





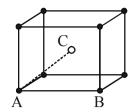


(iv) 
$$AB = a = 2R$$

$$AC = \frac{\sqrt{3} a}{2} = R + r$$

Now, 
$$\frac{R+r}{R} = \sqrt{3}$$

$$r = (\sqrt{3} - 1)R = 0.732R$$



#### **CLASS ILLUSTRATION - 02**

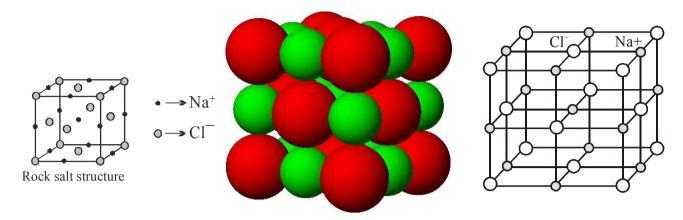
- 10. A compound is formed by two elements M and N. The element N forms ccp and atoms of M occupy 1/3rd of tetrahedral voids. What is the formula of the compound?
- 11. A solid crystallises in close packing for 'P' atoms and 25% of tetrahedral voids are occupied by 'Q' atoms. What is the simplest formula of solid?
- 12 A compound forms hexagonal close-packed structure. What is the total number of voids in 0.5 mole of it? How many of these are tetrahedral voids?
- 13. An element 'M' crystallizes in ABAB....type packing. If adjacent layer A & B are  $10\frac{\sqrt{2}}{\sqrt{3}}$  pm apart, then calculate radius of largest sphere which can be fitted in the void without disturbing the lattice arrangement (Given:  $\sqrt{2} = 1.414$ )
- 14. In compound  $M_2O_3$ , if oxide ions are in close packing while 'M' occupy the voids. Then what fraction of voids (O.V. & T.V.) left unoccupied -
- 15. An element (atomic weight = 125) crystallises in simple cubic structure. Diameter of the largest atom which can be placed without disturbing unit cell is 366 pm. If the density of element 'x' gm/cm<sup>3</sup>, the value of  $\left(\frac{6x}{5}\right)$  is

[Given:  $\sqrt{3} = 1.732$ ,  $N_A = 6 \times 10^{23}$ ]

16. What will be packing fraction of solid in which atoms are present at corners and cubic void is occupied. The insertion of the sphere into void does not disturb simple cubic lattice.

## 10.2 TYPES OF IONIC STRUCTURES:

# 10.2.1 Rock salt structure (NaCl):

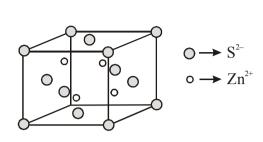


The bigger Cl<sup>-</sup> forms cubic close packing and small Na<sup>+</sup> occupy positions of all octahedral voids. The radius ratio  $\frac{r^+}{r^-}$  lie in the range 0.414 – 0.732.

- (i) Each Na<sup>+</sup> is surrounded by six Cl<sup>-</sup> and each Cl<sup>-</sup> is surrounded by six Na<sup>+</sup> ion. [6:6 coordination]
- (ii) No. of Na<sup>+</sup> and Cl<sup>-</sup> in each unit cell is 4.
- (iii) Number of formula units of NaCl per unit cell is equal to 4.
- (iv) The density of NaCl crystal is given by  $d = \left(\frac{4 \times M_{NaCl}}{N_A \times a^3}\right)$
- (v) The edge length of NaCl unit cell is given by  $(2r^+ + 2r^-) \Rightarrow \frac{\mathbf{a}}{2} = \mathbf{r}^+ + \mathbf{r}^-$

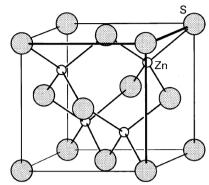
# 10.2.2 Zinc blende (sphalerite) structure (ZnS):

Larger ion (S<sup>2-</sup>) forming ccp arrangement and smaller ion (Zn<sup>2+</sup>) filling half or alternate tetrahedral voids



Zinc blende structure

- C.N. of  $Zn^{2+} = 4$ ; **(i)**
- C.N. of  $S^{2-} = 4$



[4:4 coordination]

- Formula units of ZnS per unit cell = 4. (iii)  $d_{ZnS} = \frac{4 \times M_{ZnS}}{N_A \times a^3}$  (iv)  $r_{Zn^{2+}} + r_{S^{2-}} = \frac{a\sqrt{3}}{4}$ (ii)

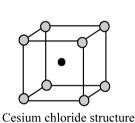
# 10.2.3 Cesium chloride structure (CsCl):

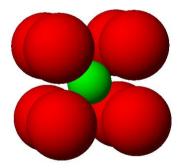
Cl<sup>-</sup> at the corners of cube and Cs<sup>+</sup> in the center (cubic void).

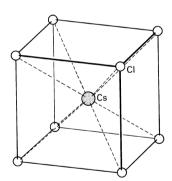
- (i) C.N. of  $Cs^+ = 8$ ;
- C.N. of  $Cl^{-} = 8$
- [8:8 coordination]
- (ii) Formula units of CsCl per unit cell = 1

(iii) 
$$d_{CsCl} = \frac{M_{CsCl}}{N_A \times a^3}$$

(iv) 
$$r_{Cs^{+}} + r_{Cl^{-}} = \frac{a\sqrt{3}}{2} \implies r^{+} + r^{-} = \frac{a\sqrt{3}}{2}$$







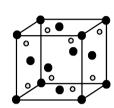
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# **10.2.4 Fluorite structure** ( $CaF_2$ ):

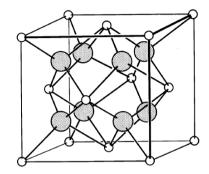
Ca<sup>2+</sup> forming ccp arrangement and F<sup>-</sup> filling all tetrahedral voids.

- (i) C.N. of  $F^- = 4$
- C.N. of  $Cs^{+} = 8$
- [8:4 coordination]

- (ii) Formula units of  $CaF_2$  per unit cell = 4
- (iii)  $d_{CaF_2} = \frac{4 \times M_{CaF_2}}{N_A \times a^3}$  (iv)  $r_{Ca^{2+}} + r_{F^-} = \frac{a\sqrt{3}}{4}$



Fluorite structure



# **10.2.5** Antifluorite structure (Li<sub>2</sub>O):

O<sup>2-</sup> ion forming ccp and Li<sup>+</sup> taking all tetrahedral voids.

(i) C.N. of  $Li^+ = 4$ 

C.N. of 
$$O^{2-} = 8$$

(ii) Formula units of  $Li_2O$ ; per unit cell = 4

(iii) 
$$d_{\text{Li}_2\text{O}} = \frac{4 \times M_{\text{Li}_2\text{O}}}{N_{\text{A}} \times a^3}$$

(iv) 
$$r_{Li^+} + r_{O^{2-}} = \frac{a\sqrt{3}}{4}$$

# **10.2.6 Corundum Structure** $(Al_2O_3)$ :

O<sup>2-</sup> forming hcp and Al<sup>3+</sup> filling 2/3 octahedral voids.



### **10.2.7 Rutile structure** (TiO<sub>2</sub>):

O<sup>2-</sup> forming hcp while Ti<sup>4+</sup> ions occupy half of the octahedral voids.

### **10.2.8 Pervoskite structure** (CaTiO<sub>3</sub>):

Ca<sup>2+</sup> in the corner of cube, O<sup>2-</sup> at the face center and Ti<sup>4+</sup> at the centre of cube.

### **10.2.9** Spinel and inverse spinel structure (MgAl<sub>2</sub>O<sub>4</sub>) :

O<sup>2-</sup> forming fcc, Mg<sup>2+</sup> filling 1/8 of tetrahedral voids and Al<sup>3+</sup> taking half of octahedral voids.

In an inverse spinel structure,  $O^{2-}$  ion form FCC lattice,  $A^{2+}$  ions occupy 1/8 of the tetrahedral voids and trivalent cation occupies 1/8 of the tetrahedral voids and 1/4 of the octahedral voids.

- Ex.4 A solid A<sup>+</sup>B<sup>-</sup> has NaCl type close packed structure. If the anion has a radius of 250 pm, what should be the ideal radius for the cation? Can a cation C<sup>+</sup> having a radius of 180 pm be slipped into the tetrahedral site of the crystal A<sup>+</sup>B<sup>-</sup>? Give reason for your answer.
- Sol. In Na<sup>+</sup>Cl<sup>-</sup> crystal each Na<sup>+</sup> ion is surrounded by 6 Cl<sup>+</sup> ions and vice versa. Thus Na<sup>+</sup> ion is placed in octahedral hole.

The limiting radius ratio for octahedral site = 0.414

$$or$$
  $\frac{A^+}{B^-} = \frac{r}{R} = 0.414$ 

Given that radius of anion  $(B^-)$  R = 250 pm

i.e. radius of cation (A<sup>+</sup>) 
$$r = 0.414 R = 0.414 \times 250 pm$$

or 
$$r = 103.5 pm$$

Thus ideal radius for cation  $(A^+)$  is r = 103.5 pm.

We know that (r/R) for tetrahedral hole is 0.225.

$$\therefore \frac{r}{R} = 0.225$$
or  $r = 0.225$   $R = 0.225 \times 250 = 56.25 \text{ pm}$ 

Thus ideal radius for cation is 56.25 pm for tetrahedral hole. But the radius of  $C^+$  is 180 pm. It is much larger than ideal radius i.e. 56.25 pm. Therefore we can not slip cation  $C^+$  into the tetrahedral site.

#### **CLASS ILLUSTRATION - 03**

- 17. Solid AB has NaCl type structure. If the radius of  $A^+$  and  $B^-$  are 0.8 Å and 1.2Å respectively and formula mass of AB is 48 g/mole, what is the density of AB solid.
  - Take: Avogadro's number =  $6 \times 10^{23}$
- 18. Calculate the value of Avagadro number from the following data:
  - Density of  $NaCl = 2.165 \text{ g cm}^{-3}$ , distance between  $Na^{+}$  and  $Cl^{-}$  ions in NaCl crystal = 281 pm. (1)
- Calculate the density (in gm/cm<sup>3</sup>) of NaCl type ionic solid (MW = 75 gm/mol) if distance between two nearest cations is  $250\sqrt{2}$  pm (avogadro number =  $6 \times 10^{23}$ )
- 20. KF crystallizes in the NaCl type structure. If the radius of  $K^+$  ion is 132 pm and that of  $F^-$  ion is 135 pm, what is the shortest K-F distance? What is the edge length of the unit cell? What is the closet  $K^+$   $K^+$  distance?
- 21. Rbl crystallizes in (8:8) structure in which each Rb<sup>+</sup> is surrounded by eight iodide ions each of radius 2.17 Å. Find the length of one side of RbI unit cell, assuming anion, anion contact.
- 22. A cubic unit cell contains manganese ions at the corners and fluoride ions at the center of each edge.
  - (a) What is the empirical formula of the compound?
  - (b) What is the co-ordination number of the Mn ion?
  - (c) Calculate the edge length of the unit cell, if the radius of Mn ion is 0.65 Å and that of  $F^-$  ion is 1.36 Å.

#### 11. IMPERFECTIONS IN SOLIDS

Although crystalline solids have short range as well as long range order in the arrangement of their constitutent particles, yet crystals are not perfect. Usually a solid consists of an aggregate of large number of small crystals. These small crystals have defects in them. This happens when crystallisation process occurs at fast or moderate rate. Single crystals are formed when the process of crystallisation occurs at extremely slow rate. Even these crystals are not free of defects.

The defects are basically irregularities in the arrangement of constituent particles. Broadly speaking, the defects are of two types, namely, **point defects** and **line defects**. Point defects are the irregularities or deviations from ideal arrangement around a point or an atom in a crystalline substance, whereas the line defects are the irregularities or deviations from ideal arrangement in entire rows of lattice points. These irregularities are called crystal defects. We shall confine our discussion to point defects only.

#### 11.1 Types of Point Defects

Point defect can be classified into three types:

- (i) Stoichiometric defects
- (ii) Non-stoichiometric defects
- (iii) Impurity added defect

#### (i) Stoichiometric Defect

These are the point defect that do not disturb the stoichiometry of the solid. They are also called *intrinsic* or **thermodynamic defects**. Basically these are of two types; vacancy defects and interstitial defect.

#### (a) Vacancy Defect:

When some of the lattice sites are vacant, the crystal is said to have vacancy defect. This results in decrease in density of the substance. This defect can also develop when a substance is heated.

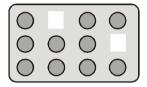


Fig.: Vacancy defects

**(b) Interstitial Defect :** When some constituent particles (atoms or molecules) occupy an interstitial site. the crystal is said to have interstitial defect. This defect increases the density of the substance.

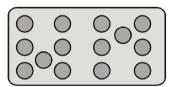


Fig.: Interstitial defects

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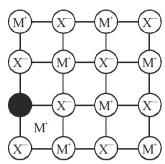
Vacancy and interstitial defects as explained above can be shown by non-ionic solids. Ionic solids must always maintain electrical neutrality. Rather than simple vacancy or interstitial defects, they show these defects as Frenkel and Schottky defects.

(c) Frenkel Defect: This defect is shown by ionic solids.

The smaller ion (usually cation) is delocalised from its normal site to an interstitial site. It creates a vacancy defect at its original site and an interstitial defect at its new location.

Frenkel defect is also called **dislocation defect**. It does not change the density of the solid.

Frenkel defect is shown by ionic substance in which there is a large difference in the size of ions, for example, ZnS, AgCl, AgBr and AgI due to small size of Zn<sup>2+</sup> and Ag<sup>+</sup> ions.



Frenkel Defect

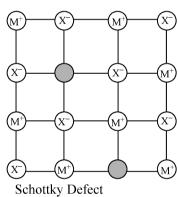
**Influences:** Makes solid crystals good conductor. In Frenkel defect, ions in interstitial sites increases the dielectric constant.

(d) Schottky Defect: It is basically a vacancy defect in ionic solids. In order to maintain electrical neutrality, the number of missing cations and anions are equal (in stoichiometric ratio)

Like simple vacancy defect, Schottky defect also

decreases the density of the substance. Number of such defects in ionic solids is quite significant. For example, in NaCl there are approximately,

10<sup>6</sup> Schottky pairs per cm<sup>3</sup> at room temperature. In 1 cm<sup>3</sup> there are about  $10^{22}$  ions. Thus, there is one Schottky defect per  $10^{16}$  ions. Schottky defect is shown by ionic substances in which the cation and anion are of almost similar sizes. For example, NaCl, KCl, CsCl and AgBr. It may be noted that AgBr shows both, Frenkel as well as Schottky defects.



**Influence:** The presence of large number of schottky defects in crystal results in significant decrease in its density.

#### (ii) Non-Stoichiometric Defects

The defects discussed so far do not disturbs the stoichiometry of the crystalline substance. However, a large number of non-stoichiometric inorganic solids are known which contain the constituent elements in non-stoichiometric ratio due to defects in their crystal structures. These defects are of two types:

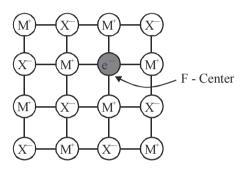
- (a) Metal excess defect.
- (b) Metal deficiency defect.

#### (a) Metal Excess Defect

#### (I) Metal excess defect due to anionic vacancies :

Alkali halides like NaCl and KCl show his type of defect. When crystals of NaCl are heated in an atmosphere of sodium vapour, the sodium atoms are deposited on the surface of the crystal. The Cl<sup>-</sup> ions diffuse to the surface of the crystal and combine with Na atoms to give NaCl. This happens by loss of electron by sodium atoms to form Na<sup>+</sup> ions.

The released electrons diffuse into the crystal and occupy anionic sites. As a result the crystal now has an excess of sodium. The anionic sites occupied by unpaired electrons are called *F-centres* (from the German word *Farbenzenter* for colour centre)



Metal excess defects due to anion vacancies

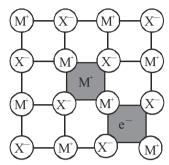
They impart yellow colour to the crystals of NaCl. The colour results by excitation of these electrons when they absorb energy from the visible light falling on the crystals. Similarly, excess of lithium makes LiCl crystals pink and excess of potassium makes KCl crystals violet (or lilac).

### (II) Metal excess defect due to the presence of extra cations at interstitial sites:

Zinc oxide is white in colour at room temperature. On heating it loses oxygen and turns yellow.

$$ZnO \xrightarrow{\text{heating}} Zn^{2+} + \frac{1}{2}O_2 + 2e^{-}$$

Now there is excess of zinc in the crystal and its formula becomes  $Zn_{1+x}O$ . The excess  $Zn^{2+}$  ions move to interstitial sites and the electrons to neighbouring interstitual sites.



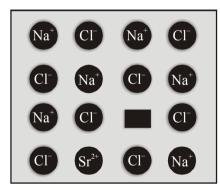
Metal excess defects due to interstitial cation

#### (b) Metal Deficiency Defect

There are many solids which are difficult to prepare in the stoichiometric composition and contain less amount of the metal as compared to the stoichiometric proportion. A typical example of this type is FeO which is mostly found with a composition of  $Fe_{0.95}O$ . It may actually range from  $FeO_{0.93}O$  to  $Fe_{0.96}O$ . In crystals of FeO, some  $Fe^{2+}$  cations are missing and the loss of positive charge is made up by the presence of required number of  $Fe^{3+}$  ions.

### (iii) Impurity Defects

If molten NaCl containing a little amount of  $SrCl_2$  is crystallised, some of the sites of Na<sup>+</sup> ions are occupied by  $Sr^{2+}$ . Each  $Sr^{2+}$  replaces two Na<sup>+</sup> Ions. It occupies the site of one ion and the other site remains vacant. The cationic vacancies thus produced are equal in number to that of  $Sr^{2+}$  ions. Another similar example is the solid solution of  $CdCl_2$  and AgCl.



Introduction of cation vacancy in

Space for Notes

NaCl by substitution of Na by Sr<sup>2</sup>

**Note:** (i) As temperature increases, no. of defects increases exponentially.

- (ii) For defect formation:  $\Delta H > 0$ ,  $\Delta S > 0$ 
  - :. More spontaneous at higher temperatures.
- (iii) No matter how many imperfections are present in a crystal, it is always electrically neutral (no net charge).

#### 12. ELECTRICAL PROPERTIES

Solids exhibit an amazing range of electrical conductivities, extending over 27 orders of magnitude ranging from  $10^{-20}$  to  $10^7$  ohm<sup>-1</sup> m<sup>-1</sup>. Solids can be classified into three types on the basis of their conductivities.

- (i) Conductors: The solids with conductivities ranging between 10<sup>4</sup> to 10<sup>7</sup> ohm<sup>-1</sup>m<sup>-1</sup> are called conductors.

  Metals having conductivities in the order of 10<sup>7</sup> ohm<sup>-1</sup>m<sup>-1</sup> are good conductors.
- (ii) Insulators: These are the solids with very low conductivities ranging between  $10^{-20}$  to  $10^{-10}$  ohm<sup>-1</sup>m<sup>-1</sup>.
- (iii) **Semiconductors**: These are the solids with conductivities in the intermediate range from  $10^{-6}$  to  $10^4$  Ohm<sup>-1</sup>m<sup>-1</sup>.

#### 12.1: Conduction of Electricity in Metals

A conductor may conduct electricity through movement of electrons or ions. Metallic conductors belong to the former category and electrolytes to the latter.

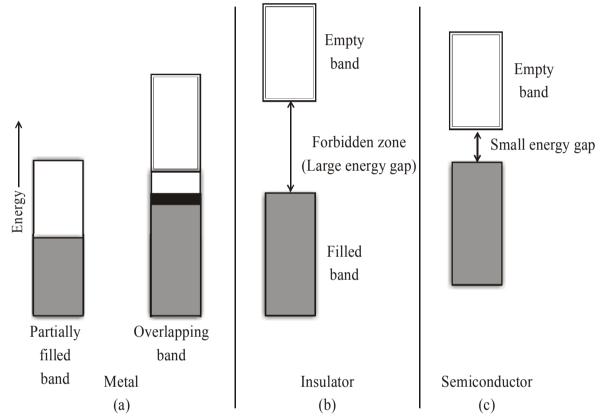
Metals conduct electricity in solid as well as molten state. The conductivity of metals depend upon the number of valence electrons available per atom. The atomic orbitals of metal atoms from molecular orbitals which are so close in energy to each other as to form a band. If this band is partially filled or it overlaps with a higher energy unoccupied conduction band, then electrons can flow easily under an applied electric field and the metal shows conductivity.

#### **12.2** : Insulator :

If the gap between filled valence band and the next higher unoccupied band (conduction band) is large, electron cannot jump to it and such a substance has very small conductivity and it behaves as an insulator.

### 12.3 : Conduction of Electricity in Semi-conductor

In case of semiconductors, the gap between the valence band and conduction band is small. Therefore, some electrons may jump to conduction band and show some conductivity. Electrical conductivity of semconductors increases with rise in temperature, since more electrons can jump to the conduction band. Substances like silicon and germanium show this type of behaviour and are called **intrinsic semiconductors**.



Distinction among (a) metals (b) insulators and (c) semiconductors.

In each case, an unshaded area represents a conduction band.

The conductivity of these interinsic semiconductors is too low to be of practical use. Their conductivity is increased by adding an appropriate amount of suitable impurity. This process is called **doping**. Doping can be done with an impurity which is electron rich or electron deficient as compared to the intrinsic semiconductor silicon or germanium. Such impurities introduce *electrical defect* in them.

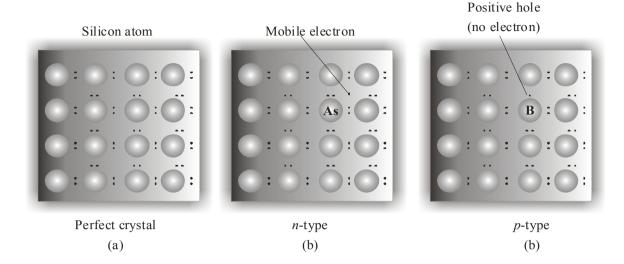
### (a) Electron – rich impurities

Silicon and germanium belong to group 14 of the periodic table and have four valence electrons each. In their crystals each atom forms four covalent bonds with its neighbours. When doped with a group 15 element like P or As, which contains five valence electrons, they occupy some of the lattice sites in silicon or germanium crystal. Four out of five electrons are used in the formation of four covalent bonds with the four neighbouring silicon atoms. The fifth electron is extra and becomes delocalised. These delocalised electrons increase the conductivity of doped silicon (or germanium). Here the increase in conductivity is due to the negatively charged electron, hence silicon doped with electron-rich impurity is called *n-type semiconductor*.

#### (b) Electron – deficit impurities

Silicon or germanium can also be doped with a group 13 element like B, Al or Ga which contains only three valence electrons. The place where the fourth valence electron is missing is called *electron hole or electron vacancy*. An electron from a neighbouring atom can come and fill the electron hole, but in doing so it would leave an electron hole at its original position. If it happens, it would appear as if the electron hole has moved in the direction opposite to that of the electron that filled it. Under the influence of electric field, electrons would move towards the positively charged plate through electronic holes, but it would appear as if electron holes are positively charged and are moving towards negatively charged plate. This type of semi conductors are called *p-type semiconductors*.

**(c)** 



### Creation of n-type and p-type semi conductors by doping groups 13 and 15 elements Applications of n-type and p-type semiconductors

Various combinations of *n*-type and *p*-type semiconductors are used for making electronic components. Diode is a combination of *n*-type and *p*-type semiconductor and is used as a rectifier. Transistors are made by sandwiching a layer of one type of semiconductor between two layers of the other type of semiconductor. *npn* and *pnp* type of transistors are used to detect or amplify radio or audio signals. The solar cell is an efficient photo-diode used for conversion of ligh energy into electrical energy.

Germinium and Silicon are group 14 elements and therefore, have a characteristic valence of four and form four bonds as in diamond. A large variety of solid state materials have been prepared by combination of group 13 and 15 or 12 and 16 to simulate average valence of four as in Ge or Si. Typical compounds of groups 13-15 are InSb, AIP and GaAs. Gallium arsenide (GaAs) semiconductor have very fast response and have revolutionised the design of semiconductor devices. ZnS, CdS, CdSe and HgTe are examples of groups 12-16 compounds. In these compounds, the bonds are not perfectly covalent and the ionic character depends on the electronegativities of the two elements.

It is interesting to learn that transition metal oxides show marked differences in electrical properties. TiO, CrO<sub>2</sub> and ReO<sub>3</sub> behave like metals. Rhenium oxide, ReO<sub>3</sub> is like metallic copper in its conductivity and appearance. Certain other oxides like VO, VO<sub>2</sub>, VO<sub>3</sub> and TiO<sub>3</sub> show metallic or insulating properties depending on temperature.

#### 13. MAGNETIC PROPERTIES:

Every substance has some magnetic properties associated with it. The origin of these properties lies in the electrons. Each electron in an atom behaves like a tiny magnet. Its magnetic moment originates from two types of motions (i) its orbital motion around the nucleus and (ii) its spin around its own axis . Electron being a charged particle and undergoing these motions can be considered as a small loop of current which possesses a magnetic moment. Thus, each electron has a permanent spin and an orbital magnetic moment associated with it. Magnitude of this magnetic moment is very small and is measured in the unit called Bohr magneton,  $\mu_{\rm B}$ . It is equal to  $9.27 \times 10^{-24} A~{\rm m}^2$ .

On the basis of their magnetic properties, substances can be classified into five categories: (i) paramagnetic (ii) diamagnetic (iii) ferromagnetic (iv) antiferromagnetic and (v) ferrimagnetic.

- (i) **Paramagnetism**: Paramagnetic substances are weakly attracted by a magnetic field. They are magnetised in a magnetic field in the same direction. They lose their magnetism in the absence of magnetic field. Paramagnetism is due to presence of one or more unpaired electrons which are attracted by the magnetic field. O<sub>2</sub>, Cu<sup>2+</sup>, Fe<sup>3+</sup>, Cr<sup>3+</sup> are some examples of such substances.
- (ii) **Diamagnetism:** Diamagnetic substances are weakly repelled by a magnetic field. H<sub>2</sub>O, NaCl and C<sub>6</sub>H<sub>6</sub> are some examples of such substances. They are weakly magnetised in a magnetic field in opposite direction. Diamagnetism is shown by those substances in which all the electrons are paired and there are no unpaired electrons. Pairing of electrons cancels their magnetic moments and they lose their magnetic character.
- (iii) **Ferromagnetism:** A few substances like iron, cobalt, nickel, gadolinium and CrO<sub>2</sub> are attracted very strongly by a magnetic field. Such substances are called ferromagnetic substances. Besides strong attractions, these substances can be permanently magnetised. In solid state, the metal ions of ferromagnetic substances are grouped together into small regions called *domains*. Thus, each domain acts as a tiny magnet. In an unmagnetised piece of a ferromagnetic substance the domains are randomly oriented and their magnetic moments get cancelled. When the substance is placed in a magnetic field all the domains get oriented in the direction of the magnetic field and a strong magnetic effect is produced. This ordering of domains persist even when the magnetic field is removed and the ferromagnetic substance becomes a permanent magnet.

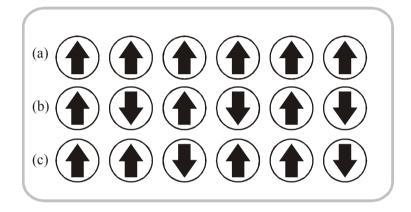
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### (iv) Antiferromagnetism:

Substances like MnO showing antiferromagnetism have domain structure similar to ferromagnetic substance, but their domains are oppositely oriented and cancel out each other's magnetic moment

### (v) Ferrimagnetism:

Ferrimagnetism is observed when the magnetic moments of the domains in the substance are aligned in parallel and anti-parallel directions in unequal numbers. They are weakly attracted by magnetic field as compared to ferromagnetic substances. Fe $_3$ O $_4$  (magnetite) and ferrites like MgFe $_2$ O $_4$  and ZnFe $_2$ O $_4$  are examples of such substances. These substances also lose ferrimagnetism on heating and become paramagnetic.



Schematic alignment of magnetic moments in (a) ferromagnetic (b) antiferromagnetic and (c) ferrimagnetic



### **CLASS ILLUSTRATION - 04**

- 23. A crystal of NaCl, which has sodium ions and chloride ions missing from the lattice point, is said to exhibit
  - (A) Surface defect
- (B) Lattice defect
- (C) Frenkel defect
- (D) Schottky defect
- 24. A piece of copper and another of Ge are cooled from room temperature to 80 K. The resistance of:
  - (A) each of them increases
  - (B) Cu increases and that of Ge decreases
  - (C) Cu decreases and that of Ge increases
  - (D) each of them decreases
- 25. The composition of a sample of wustite is  $Fe_{0.93}O_{1.0}$ . What percentage of iron is present in the form of Fe(III)?
- An element X (atomic weight = 24 gm/mole) forms a face centred cubic lattice. If the edge length of the lattice is  $4 \times 10^{-8}$  cm and the observed density is  $2.40 \times 10^{3}$  kg/m³, calculate the percentage occupancy of lattice points by X element. (Given:  $N_A = 6 \times 10^{23}$ )
- 27. AgCl has the same structure as that of NaCl. The edge length of unit cell of AgCl is found to be 523.5 pm and the density of AgCl is  $6.0 \text{ g cm}^{-3}$ . Find the percentage of sites that are unoccupied.  $[Ag = 108, (5.235)^3 = 143.5]$
- 28. The pyknometric density of sodium chloride crystal is  $2.165 \times 10^3$  kg m<sup>-3</sup> while its X-ray density is  $2.178 \times 10^3$  kg m<sup>-3</sup>. The fraction of unoccupied sites in sodium chloride crystal is:

[Hint: Fraction of unoccupied sites

$$= \frac{X - \text{ray density} - \text{pyknometric density}}{X - \text{ray density}} J$$

### **ANSWER KEY**

### **CLASS ILLUSTRATION - 01**

1. Ans. $X_2Y_3$ 

2. Ans.  $2.81 \times 10^{-23}$  cm<sup>3</sup>

3. **Ans.** r = 1.136 Å

4. Ans.  $\ell = 4.0 \times 10^{-8} \text{ cm}$ 

- 5. Ans. 4
- 6. Ans.(a) 4.5 Å, (b) 5.2 Å, (c) 8, (d) 6, (e) 0.929 g/cm<sup>3</sup>
- 7.  $Ans.41.67 g cm^{-3}$

8. Ans.Ans.8

9.  $Ans.5 \times 10^{24}$ 

### **CLASS ILLUSTRATION - 02**

10. Ans.  $N_3M_2$ .

11.  $Ans. P_2Q$ 

12 Ans. 1 mol.

13. Ans.(2.07 pm)

14. Ans.  $(\frac{7}{9})$ 

15. Ans.(2)

16. Ans.0.72

### **CLASS ILLUSTRATION - 03**

17.  $Ans.(5 \text{ gm/cm}^3)$ 

18.  $Ans.6.09 \times 10^{23}$ 

19. Ans (4)

20. Ans.267 pm, 534 pm, 377.6 pm

21. Ans.4.34 Å

22. Ans.(a) MnF<sub>3</sub>, (b) 6, (c) 4.02Å

### **CLASS ILLUSTRATION - 04**

23. Ans.(D)

24. Ans.(C)

25. Ans.15.05 %

26 96% Ans.

27. Ans.10

28.  $Ans.5.96 \times 10^{-3}$ 

### PREVIOUS YEARS SOLVED QUESTION

1. A metal cryatallises into two cubic phases, FCC and BCC whose unit cell lengths are 3.5 and 3.0 Å respectively. Calculate the ratio of densities of FCC and BCC. [JEE-1999]

Ans. 1.259

Sol.  $\rho_{\text{Fcc}} = \frac{4 \times M}{N_A \times \left(3.5 \times 10^{-10}\right)^3}$ 

 $\rho_{\text{Bcc}} = \frac{2 \times M}{N_A \times \left(3 \times 10^{-10}\right)^3}$ 

 $\frac{\rho_{Fcc}}{\rho_{Bcc}} = \frac{4}{2} \times \left(\frac{3}{3.5}\right)^3$ = 1.259

2. The coordination number of a metal crystallising in a hcp structure is

[JEE-2000]

- (A) 12
- (B)4
- (C) 8
- (D) 6

Ans. (A)

Sol. Theory Based

3. In any ionic solid [MX] with schottky defects, the number of positive and negative ions are same.

[T/F]

[JEE-2000]

Ans. True

Sol. Theory Based

- 4. In a solid "AB" having NaCl structure "A" atoms occupy the corners of the cubic unit cell. If all the face-centred atoms along one of the axes are removed, then the resultant stoichiometry of the solid is
  - (A) AB,
- (B) A<sub>2</sub>B
- $(C) A_{4}B_{3}$
- (D)  $A_3B_4$
- [JEE-2000]

Sol.

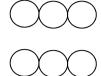
 $Z_{A} = 8 \times \frac{1}{8} + 4 \times \frac{1}{2} = 3$   $Z_{B} = 1 + 12 \times \frac{1}{4} = 4$   $A_{3}B_{4}$ 

5. The figures given below show the location of atoms in three crystallographic planes in FCC lattice. Draw the unit cell for the corresponding structure and identify these planes in your diagram.

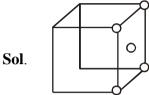
[JEE-2000]







Ans.



fcc plan







- A substance  $A_x B_y$  crystallises in a FCC lattice in which atoms "A" occupy each corner of the cube and atoms "B" occupy the centres of each face of the cube. Identify the correct composition of the substance  $A_x B_y$ .
  - (A) AB<sub>3</sub>

 $(B) A_{4}B_{3}$ 

(C) A<sub>3</sub>B

(D) composition cannot be specified [JEE-2002]

Ans. (A)

Sol. AB<sub>3</sub>

7. Marbles of diameter 10 mm each are to be arranged on a flat surface so that their centres lie within the area enclosed by four lines of length each 40 mm. Sketch the arrangement that will give the maximum number of marbles per unit area, that can be enclosed in this manner and deduce the expression to calculate it.

[JEE 2003]

**Ans.** 18

$$\frac{n \times \pi r^2}{a^2} = \frac{\pi}{2\sqrt{3}}$$
$$\frac{n \times \pi 5^2}{40 \times 40} = \frac{\pi}{2\sqrt{3}}$$

$$n = 18.475$$

- 8.
  - (i) AB crystallizes in a rock salt structure with A: B=1:1. The shortest distance between A and B is  $Y^{1/3}$  nm. The formula mass of AB is 6.023 Y amu where Y is any arbitrary constant. Find the density in kg m-3.
    - (ii) If measured density is 20 kg m<sup>-3</sup>. Identify the type of point defect.

[JEE-2004]

shortest distance b/w A & B =  $Y^{1/3}$  nm Sol.

$$a = 2Y^{1/3}$$

$$\rho = \frac{4 \! \times \! 6.023 Y \! \times \! 10^{-3}}{6.023 \! \times \! 10^{23} \! \times \! \left[ 2 Y^{1/3} \! \times \! 10^{-9} \right]^{\!3}}$$

$$\rho = \frac{4 \times 10^{-3}}{8 \times 10^{-4}}$$
$$= 5 \text{ kgm}^{-3}$$

- copy statement for answer Key (ii)
- 9. Which of the following FCC structure contains cations in alternate tetrahedral voids?
  - (A) NaCl
- (B) ZnS
- (C) Na<sub>2</sub>O
- (D) CaF,

[JEE 2005]

- **(B)** Ans.
- **10.** An element crystallises in FCC lattice having edge length 400 pm. Calculate the maximum diameter which can be placed in interstital sites without disturbing the structure. [JEE 2005]
- 117.1 pm Ans.

**Sol**. 
$$\sqrt{2}$$
 a = 4r

$$r = \frac{\sqrt{2}a}{4}$$

for octahedral void

$$r^1 = .414 \times 141.4$$

$$d = 2r^1$$

$$= 117.07$$

Space for Notes

lattice. If the density is 2 g/cc then find the radius of metal atom. ( $N_A = 6 \times 10^{23}$ ). Give the answer in pm.

216.5 pm Ans.

**Sol.** 
$$a = 5 \text{Å}$$

11.

$$M = 75 \text{ gram/mol}$$

$$d = 2 \text{ gram/cm}$$

$$2 = \frac{Z \times 75}{\left(6.02 \times 10^{+23}\right) \left(5 \times 10^{-8}\right)^3}$$

$$Z = 2$$
 (Bcc)

$$\sqrt{3}$$
 a = 4r

$$r = \frac{\sqrt{3}a}{4} = 2.165$$
Å

12. Match the crystal system / unit cells mentioned in Column I with their characteristic features mentioned in Column II. Indicate your answer by darkening the appropriate bubbles of the  $4 \times 4$  matrix given in the OMR.

The edge length of unit cell of a metal having atomic weight 75 g/mol is 5 Å which crystallizes in cubic

Column I

- (A) simple cubic and face-centred cubic
- (B) cubic and rhombohedral
- (C) cubic and tetragonal
- (D) hexagonal and monoclinic

Column II

- (P) have these cell parameters a = b = cand  $\alpha = \beta = \gamma$
- (Q) are two crystal systems
- (R) have only two crystallographic angles of 90°
- (S) belong to same crystal system.

[JEE 2007]

(A) P, S; (B) - P, Q; (C) - Q; (D) - Q, R

### Paragraph for Ouestion No. 13 to 15

In hexagonal systems of crystals, a frequently encountered arrangement of atoms is described as a hexagonal prism. Here, the top and bottom of the cell are regular hexagons and three atoms are sandwiched in between them. A space-filling model of this structure, called hexagonal close-packed (HCP), is constituted of a sphere on a flat surface surrounded in the same plane by six identical spheres as closely as possible. Three spheres are then placed over the first layer so that they touch each other and represent the second layer. Each one of these three spheres touches three spheres of the bottom layer. Finally, the second layer is covered with a third layer that is identical to the bottom layer in relative position. Assume radius of every sphere to be 'r'.

13. The number of atoms in this HCP unit cells is [JEE 2008]

- (A) 4
- (B)6
- (C) 12
- (D) 17

**(B)** Ans.

- $12 \times \frac{1}{6} + 2 \times \frac{1}{2} + 3 \times 1 = 6$  atoms Sol.
- 14. The volume of this HCP unit cell is

[JEE 2008]

- (A)  $24\sqrt{2} r^3$  (B)  $16\sqrt{2} r^3$  (C)  $12\sqrt{2} r^3$
- (D)  $\frac{64}{3\sqrt{3}}$  r<sup>3</sup>

Ans. (A)

$$Sol. V = \frac{6\sqrt{3}a^3}{4} \times C$$

$$a = 2r$$

$$C = \frac{4\sqrt{2}r}{\sqrt{3}}$$

$$V = 24\sqrt{2}r^3$$

**15.** The empty space in this HCP unit cell is [JEE 2008]

- (A)74%
- (B) 47.6 %
- (C) 32%
- (D) 26%

Ans. **(D)** 

Space for Notes

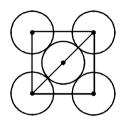
**16.** The correct statement(s) regarding defects in solid is (are)

[JEE 2009]

- (A) Frenkel defect is usually favoured by a very small difference in the sizes of cation and anion.
- (B) Frenkel defect is a dislocation defect
- (C) Trapping of an electron in the lattice leads to the formation of F-center.
- (D) Schottky defects have no effect on the physical properties of solids.

Ans. (B,C)

17. The packing effeciency of the two-dimensional square unit cell shown below is [JEE-2010]



- (A) 39.27%
- (B) 68.02%
- (C) 74.05%
- (D) 78.54%

Ans. (D)

**Sol.** 
$$PF = \frac{2\pi r^2}{\left(\frac{4r}{\sqrt{2}}\right)^2} = .785$$

$$\% \text{ PF} = 78.5\%$$

Ε

#### EXERCISE # S-I

#### **METALLIC CRYSTALS**

#### Cubic crystals

- 1. A closed packed structure of uniform spheres has the edge length of 600 pm. Calculate the radius of sphere, if it exist in  $(\sqrt{2} = 1.4, \sqrt{3} = 1.7)$ 
  - (a) simple cubic lattice
- (b) BCC lattice
- (c) FCC lattice
- 2. Xenon crystallises in the face-centred cubic lattice and the edge length of the unit cell is  $438\sqrt{2}$  pm. What is the nearest neighbour distance and what is the radius of xenon atom?
- 3. The effective radius of the iron atom is  $\sqrt{2}$  Å. It has FCC structure. Calculate its density (Fe = 56 amu ,  $N_A = 6 \times 10^{23}$ )
- **4.** Calculate the ratio of densities if same element undergoes fcc as well as simple cubic packing. Assume same atomic radius in both crystals.
- Potassium has body-centred cubic structure with the nearest neighbour distance  $260\sqrt{3} \text{ pm}$ . Its density would be  $(\frac{1}{(5/2)^2} = 0.036 \text{ , N}_A = 6 \times 10^{23}, \text{ K} = 39)$
- A cubic solid is made up of two elements 'A' and 'B'. Atoms 'B' are at the corners of the cube and 'A' at the body centre. What is the simplest formula of compound?
- 7. An element 'X' crystallizes in bcc. Find volume of unit cell in  $(\mathring{A})^3$ , if atomic radius is  $\sqrt{3}$   $\mathring{A}$ .
- **8.** A lattice has simple cube unit cell then number of faces which meets at a corner of a cube in this lattice is.
- **9.** How many next nearest neighbours does potassium have in bcc lattice?

### PACKING IN SOLIDS

- **10.** A cubic solid is made by atoms 'A' forming close pack arrangement, 'B' occupying one-fourth of tetrahedral void and C occupying half of the octahedral voids. What is the formula of compound?
- 11. If number of nearest neighbours, next nearest ( $2^{nd}$  nearest) neighbour and next to next nearest ( $3^{rd}$  nearest) neighbours are x, y and z respectively for body centred cubic unit cell, then calculate value of  $\frac{xy}{z}$  is.
- **12.** In FCC unit cell, what fraction of edge is not covered by atoms?
- 13. For ABC ABC ABC .... packing, distance between two succesive tetrahedral void is X and distance

between two successive octahedral void is y in an unit cell, then  $\frac{y\sqrt{2}}{X}$  is

#### **IONIC CRYSTALS**

14. If the radius of Mg<sup>2+</sup> ion, Cs<sup>+</sup> ion, O<sup>2-</sup> ion, S<sup>2-</sup> ion and Cl<sup>-</sup> ion are 0.65 Å, 1.69 Å, 1.40 Å, 1.84 Å, and 1.81 Å respectively, calculate the co-ordination numbers of the cations in the crystals of MgS, MgO and CsCl.

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**15.** The two ions A<sup>+</sup> and B<sup>-</sup> have radii 88 pm and 200 pm respectively. In the closed packed crystal of compound AB, predict the co-ordination number of A<sup>+</sup>.

- Spinel is a important class of oxides consisting of two types of metal ions with the oxide ions arranged in CCP pattern. The normal spinel has one-eight of the tetrahedral holes occupied by one type of metal ion and one half of the octahedral hole occupied by another type of metal ion. Such a spinel is formed by  $Zn^{2+}$ ,  $Al^{3+}$  and  $O^{2-}$ , with  $Zn^{2+}$  in the tetrahedral holes. Give the formula of spinel.
- 17. CsCl has bcc unit cell with edge length 400 pm. Calculate the interionic distance in CsCl.
- 18. The density of KBr is 2.38 g cm<sup>-3</sup>. The length of the edge of the unit cell is 700 pm. Find the number of fomula unit of KBr present in the single unit cell.

$$(N_A = 6 \times 10^{23} \text{ mol}^{-1}, \text{At. mass} : K = 39, \text{Br} = 80)$$

- 19. A crystal of lead(II) sulphide has NaCl structure. In this crystal the shortest distance between  $Pb^{+2}$  ion and  $S^{2-}$  ion is 300 pm. What is the length of the edge of the unit cell in lead sulphide? Also calculate the unit cell volume.
- 20. If the length of the body diagonal for CsCl which crystallises into a cubic structure with Cl<sup>-</sup> ions at the corners and Cs<sup>+</sup> ions at the centre of the unit cell, is 7 Å and the radius of the Cs<sup>+</sup> ion is 1.69 Å, what is the radius of Cl<sup>-</sup> ion?

#### PROBLEMS RELATED WITH DEFECTS IN SOLID

- 21. If NaCl is dopped with  $10^{-3}$  mol % SrCl<sub>2</sub>, what is the number of cation vacancies per mole of NaCl?  $(N_{\Delta} = 6 \times 10^{23})$
- 22. A non stoichiometric compound  $Fe_7S_8$  consist of iron in both  $Fe^{+2}$  and  $Fe^{+3}$  form and sulphur is present as sulphide ions. Calculate cation vacancies as a percentage of  $Fe^{+2}$  initially present in the ideal crystal.
- 23. The density of ZnS crystal (Zinc blende structure) having 10% Frenkel defect is

[ 
$$r_{Zn^{2+}} = 40\sqrt{3}pm, r_{S^{2-}} = 110\sqrt{3}pm, Zn = 65.2, S = 32$$
 ]

# EXERCISE # S-II

- 1. The density of diamond from the fact that it has face centred cubic structure with two atoms per lattice point and unit cell edge length of 3.6 Å, is 'x' gm / cm<sup>3</sup>, then the value of (1.458x) is  $(N_A = 6 \times 10^{23})$
- 2. What is the percent by mass of titanium in rutile, a mineral that contain titanium and oxygen, if structure can be described as a closest packed array of oxide ions, with titanium in one half of the octahedral holes. What is the oxidation number of titanium? (Ti = 48)
- 3. The mineral hawleyite, one form of CdS, crystallizes in one of the cubic lattices, with edge length 5.87Å. The density of hawleyite is  $4.63 \text{ g cm}^{-3}$ . (Cd = 112)
  - (i) In which cubic lattice does hawleyite crystallize?
  - (ii) Find the Schottky defect in g cm<sup>-3</sup>.
- **4.** KCl crystallizes in the same type of lattice as does NaCl. Given that  $\frac{r_{Na^+}}{r_{Cl^-}} = 0.5$  and  $\frac{r_{Na^+}}{r_{K^+}} = 0.7$  Calculate:
  - (a) The ratio of the sides of unit cell for KCl to that for NaCl and
  - (b) The ratio of densities of NaCl to that for KCl.

$$\left( \left( \frac{8}{7} \right)^3 = 1.5, \frac{74.5}{58.5} = 1.25 \right)$$

# EXERCISE # O-I

# SINGLE CORRECT:

_			stances and axial angles for rhombohedral system?			
	(A) $a = b = c$ , $\alpha = \beta$			(B) $a = b \neq c$ , $\alpha = \beta = \gamma = 90^{\circ}$		
_	(C) $a \neq b = c$ , $\alpha = \beta$		(D) $a \neq b \neq c$ , $\alpha \neq \beta \neq c$	$\neq \gamma \neq 90^{\circ}$		
2.	$a \neq b \neq c, \alpha \neq \beta \neq \gamma \neq \alpha$	<del>-</del>	_, _ , _ , _ , _ , _ , _ , _ , _ , _ ,			
	(A) tetragonal system		(B) orthorhombic syst	tem		
_	(C) monoclinic system		(D) triclinic system			
<b>3.</b>	Diamond belongs to		(0)	(T) 1		
	(A) Cubic	(B) triclinic	(C) tetragonal	(D) hexagonal		
4.	A match box exhibits	S <b>-</b>	(D) M 1: :			
	(A) Cubic geometry		(B) Monoclinic geom	=		
	(C) Tetragonal geom	•	(D) Orthorhombic geo	-		
5.	Which of the following solids substances will have same refractive index when measured in different directions?					
	(A) NaCl		(B) Monoclinic sulph	(B) Monoclinic sulphur		
	(C) Rubber		(D) Graphite			
6. An ionic compound has a unit cell consisting of A ions at the corners of a cube and E				s of a cube and B ions on the		
	centres of the faces of the cube. The empirical formula of this compound would be-[AIEEE-05]					
	(A) A <sub>2</sub> B	(B) AB	$(C) A_3 B$	(D) AB <sub>3</sub>		
7.	· · · <u>2</u>	` '		` '		
7. In the body-centred cubic unit cell & face centred cubic unit cell, the rallengh(a) of the unit cell is respectively:				adias of atom in terms of eage		
	0 0	2 /22	[2 <sub>0</sub> 0	$\sqrt{2}$		
	(A) $\frac{a}{2}$ , $\frac{a}{2\sqrt{2}}$	(B) $\frac{a}{2\sqrt{2}}, \frac{\sqrt{3}a}{4}$	(C) $\frac{\sqrt{3}a}{4}$ , $\frac{a}{2\sqrt{2}}$	(D) $\frac{\sqrt{3}a}{2}$ , $\frac{a}{2\sqrt{2}}$		
8.	Crystal system in wh	ich maximum number o	of Bravais lattices are po	ssible is		
	(A) Cubic	(B) Triclinic	(C) Orthorhombic (D) Rhombohedral			
9.	Number of atoms at	second nearest position	from a given atom in a	BCC structure is		
	(A) 8	(B) 6	(C) 12	(D) 4		
10.	Percentage area of ea	ach face covered by ato	ms in a FCC unit cell is	-		
	(A) 60.4%	(B) 68%	(C) 74%	(D) 78.5%		
11.	Correct sequence of the coordination number in SC, FCC & BCC is-					
	(A) 6, 8, 12	(B) 6, 12, 8	(C) 8, 12, 6	(D) 8, 6, 12		
12.	The no. of atoms per	unit cell in B.C.C. & F.	C.C. is respectively:	[AIEEE-02]		
	(A) 8, 10	(B) 2, 4	(C) 1, 2	(D) 1, 3		
13.	T 1 1 0 1					
	Total volume of ator	ns present in a face-cent	tred cubic unit cell of a r	netal is (r is atomic radius):		

(A)  $\frac{24}{3}\pi r^3$  (B)  $\frac{12}{3}\pi r^3$  (C)  $\frac{16}{3}\pi r^3$ 

(D)  $\frac{20}{3}\pi r^3$ 

				John State				
14.	Percentages of free space in cubic close packed structure and in body centred packed structure are							
	respectively:-			[AIEEE-10]				
	(A) 48% and 26%	(B) 30% and 26%	(C) 26% and 32%	(D) 32% and 48%				
15.	If 'Z' is the number	of atoms in the unit	cell that represents th	e closest packing sequence				
	A B C A B C, the number of tetrahedral voids in the unit cell is equal to							
	(A) Z	(B) 2Z	(C) Z/2	(D) Z/4				
16.	The interstitial hole is	called tetrahedral becau	se					
	(A) It is formed by four spheres.							
	(B) Partly same and partly different.							
	(C) It is formed by for	(C) It is formed by four spheres the centres of which form a regular tetrahedron.						
	(D) None of the above	e three.						
17.	The size of an octahedral void formed in a closest packed lattice as compared to tetrahedral void is							
	(A) Equal	(B) Smaller	(C) Larger	(D) Not definite				
18.	` '	If the anions (A) form hexagonal closest packing and cations (C) occupy only 2/3 octahedral voids in						
		mula of the compound i						
	(A) CA	(B) CA <sub>2</sub>	$(C) C_2 A_3$					
19.	In a compound, atoms of element Y form ccp lattice and those of element X occupy 2/3 <sup>rd</sup> of tetrahedral							
	voids. The formula of	the compound will be -		[AIEEE-08]				
	$(A) X_4 Y_3$	(B) $X_2Y_3$	(C) $X_2Y$	(D) $X_{3}Y_{4}$				
20.	In fcc unit cell smallest distance between octahedral void & tetrahedral void is -							
	(a = edge length of unit cell)							
	а	$\sqrt{2}$ o		./2 0				
	(A) $\frac{a}{\sqrt{2}}$	(B) $\frac{\sqrt{3}  a}{2}$	(C) a	(D) $\frac{\sqrt{3} a}{4}$				
21.	What is not true regard	ding hexagonal close pa	icking (hen)	•				
<b>41</b> •	(A) packing fraction is	0 0	teking (nep)					
	(B) coordination num							
	(C) ABC ABCtype packing							
22	` '	etrahedral and octahedra						
22.	In which of the following arrangement distance between two nearest neighbours is maximum, considering identical sized atoms in all arrangements?							
	_	_		(D)1 :11				
	(A) Simple cubic	(B) bcc	(C) fcc	(D) equal in all				
23.	•	re there in 1 gram cubic	•					
	(A) $\frac{4 \times N_A}{50.5}$	(B) $\frac{N_A}{50.5}$	(C) $\frac{N_A}{58.5 \times 4}$	(D) $\frac{N_A}{50.5 - 0}$				
24.			58.5×4 aped ideal crystal of Na					
	(A) $1.28 \times 10^{21}$ unit c	-	(B) $1.71 \times 10^{21}$ unit c	•				
	(11) 1.20 10 unit 0	<b>V</b> 110	(2) 1./1 10 unit					

(D)  $5.14 \times 10^{21}$  unit cells

E

(C)  $2.57 \times 10^{21}$  unit cells

25.	The edge length of a face centred cubic cell of an ionic substance is 508 pm. If the radius of the cation						
	is 110 pm, the radius	of the anion is :-		[AIEEE-10]			
	(A) 144 pm	(B) 288 pm	(C) 398 pm	(D) 618 pm			
26.		nber of cation and anion					
		(B) 6:3 and 4:4					
27.	A compound XY crys	stallizes in 8:8 lattice wi	ith unit cell edge lenght	of 480 pm. If the radius of Y			
	is 225 pm, then the ra-	dius of X <sup>+</sup> is					
	(A) 127.5 pm		(B) 190.68 pm	(C) 225 pm			
20	(D) 255 pm	1 of CoCl company and sto					
28.		l of CsCl corresponds to (B) 1 Cs <sup>+</sup> and 6 Cl <sup>-</sup>		(D) & Cs <sup>+</sup> and 1 Cl <sup>-</sup>			
29.				.5 pm, then the ideal radius of			
	B <sup>-</sup> would be	ib has Zho type stractar	c. 11 the fadius 11 15 22.	o pin, then the lacar radius of			
		(B) 100 pm	(C) 145.16 pm	(D) none of these			
30.	Edge length of M <sup>+</sup> X <sup>-</sup> (	NaCl structure) is 7.2 Å.	Assuming M <sup>+</sup> – X <sup>-</sup> cont	tact along the cell edge, radius			
	of $X^-$ ion is $(r_{M^+} = 1.6a)$	of $X^-$ ion is $(r_{M^+} = 1.6 \text{Å})$ :					
	(A) 2.0 Å	(B) 5.6 Å	(C) 2.8 Å	(D) 38 Å			
31.	NH <sub>4</sub> Cl crystallizes in	CsCl type lattice with a u	unit cell edge length of 3	387 pm. The distance between			
	the oppositively charg	the oppositively charged ions in the lattice is					
	(A) 335.1 pm	(B) 83.77 pm	(C) 274.46 pm	(D) 137.23 pm			
32.	$r_{Na^+} = 95$ pm and $r_{Cl^-} = 181$ pm in NaCl (rock salt) structure. What is the shortest distance Na <sup>+</sup> ions?						
	(A) 778.3 pm	(B) 276 pm	(C) 195.7 pm	(D) 390.3 pm			
33.	AB crystallises itself	as NaCl crystal. If r <sub>+</sub> =	$\frac{2}{\sqrt{6}}$ and $r_{-} = \sqrt{6}$ , the 6	edge length of cube is			
	(A) - F	(P) 4	8	(D) 16			
	(A) $2\sqrt{3}$	(B) $\frac{4}{\sqrt{3}}$	(C) $\frac{8}{\sqrt{6}}$	(D) $\frac{16}{\sqrt{6}}$			
34.	Which of the follow	ing is the most likely to	show schottky defect ?				
J <b>T</b> •	(A) CaF <sub>2</sub>	(B) ZnS	(C) AgCl	(D) CsCl			
35.	<u>~</u>	ct, in AB type ionic solid	· / •	( ,			
		(A) cations are missing from the lattice sites and occupy the interstitial sites					
		cations and anions are n	_				
	(C) anions are missing and electrons are present in their place						

(D) equal number of extra cations and electrons are present in the interstitial sites

(B) Number of nearest Na<sup>+</sup> ions of another Na<sup>+</sup> in Na<sub>2</sub>O crystal will be 24.

nearest atom of face each other in fcc lattice

'a' is length of edge of unit cell

(A) Two adjacent face centre atom doesn't touch each other in fcc unit cell because they are not

(C) Minimum distance between two cubical voids in simple cube unit cell lattice will be 'a' where

(D) By defects in solids, density of solids either remains constant or decreases but it can never

Choose the correct option.

increase.

**36.** 

,							
<b>37.</b>	The measured density of AgI is $6.94~\text{g/cm}^{-3}$ and the theoretical density is $5.67~\text{g/cm}^{-3}$ . These data indicates						
	that solid A	AgI has -					
	(A) Schottky defect				(B) Frenkel defect		
	(C) Interst	itial impuri	ties defect		(D) Bo	th (A) and (B)	
38.	Which of	the followi	ing stateme	ent is CORI	RECT?		
	(A) A me	(A) A metal can show only non- stoichiometric defects					
	(B) Schot	(B) Schottky defect reduces the density of a solid due to significant increase in volume.					
	(C) Impur	(C) Impurity defect always change the density.					
	(D) Solids	(D) Solids having F-centres may have metal excess defect due to missing anions.					
39.	What type of crystal defect is indicated in the diagram below?				below?	[AIEEE-04]	
	Na <sup>+</sup>	Cl <sup>-</sup>	$Na^+$	Cl <sup>-</sup>	$Na^+$	C1 <sup>-</sup>	
	Cl <sup>-</sup>		Cl-	$Na^+$		Na <sup>+</sup>	
	Na <sup>+</sup>	Cl <sup>-</sup>		Cl <sup>-</sup>	$Na^+$	Cl <sup>-</sup>	
	Cl-	Na	+C1-	Na <sup>+</sup>		$Na^+$	
	(A) Frenkel defect			(B) Sch	(B) Schottky defect		
	(C) Interstitial defect (D) Frenkel and Schottky				nkel and Schottky d	lefects	
40.	Lattice e	energy of ar	n ionic com	nound dene	nds upon -		[AIEEE-05]

(A) Size of the ion only

- (B) Charge on the ion only
- (C) Charge on the ion and size of the ion
- (D) Packing of ions only

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### EXERCISE # O-II

#### **SINGLE CORRECT:**

- 1. The only incorrect statement for the packing of identical spheres in two dimension is:
  - (A) For square close packing, coordination number is 4.
  - (B) For hexagonal close packing, coordination number is 6.
  - (C) There is only one void per atom in both, square and hexagonal close packing.
  - (D) Hexagonal close packing is more efficiently packed than square close packing.
- 2. Which of the following statements is correct in the rock-salt structure of an ionic compounds?
  - (A) coordination number of cation is four whereas that of anion is six.
  - (B) coordination number of cation is six whereas that of anion is four.
  - (C) coordination number of each cation and anion is four.
  - (D) coordination number of each cation and anion is six.
- **3.** Which one of the following schemes of ordering closest packed sheets of equal sized spheres do not generate close packed lattice.
  - (A) ABCABC
- (B) ABACABAC
- (C) ABBAABBA
- (D) ABCBCABCBC
- **4.** Copper metal crystallizes in FCC lattice. Edge length of unit cell is 362 pm. The radius of largest atom that can fit into the voids of copper lattice without disturbing it is
  - (A) 53 pm
- (B) 45 pm
- (C) 93 pm
- (D) 93 pm
- 5. Packing fraction in 2-D hexagonal arrangement of identical sphere is
  - (A)  $\frac{\pi}{3\sqrt{2}}$
- (B)  $\frac{\pi}{3\sqrt{3}}$
- (C)  $\frac{\pi}{2\sqrt{3}}$
- (D)  $\pi/6$
- The density of  $CaF_2$  (fluorite structure) is 3.18 g/cm<sup>3</sup>. The length of the side of the unit cell is (Ca = 40, F = 19)
  - (A) 253 pm
- (B) 344 pm
- (C) 546 pm
- (D) 273 pm

- **7.** Choose the correct option.
  - (A) Two adjacent face centre atom doesn't touch each other in fcc unit cell because they are not nearest atom of face each other in fcc lattice
  - (B) Number of nearest Na<sup>+</sup> ions of another Na<sup>+</sup> in Na<sub>2</sub>O crystal will be 24.
  - (C) Minimum distance between two cubical voids in simple cube unit cell lattice will be 'a' where 'a' is length of edge of unit cell
  - (D) By defects in solids, density of solids either remains constant or decreases but it can never increase.

#### **MORE THAN ONE MAY BE CORRECT:**

- **8.** Lead metal has a density of  $11.34 \text{ g/cm}^3$  and crystallizes in a face–centred lattice. Choose the correct alternatives (Pb = 208, N<sub>A</sub> =  $6 \times 10^{23}$ )
  - (A) the volume of one unit cell is  $1.22 \times 10^{-22}$  cm<sup>3</sup>.
  - (B) the volume of one unit cell is  $1.22 \times 10^{-19}$  cm<sup>3</sup>.
  - (C) the atomic radius of lead is 175 pm.
  - (D) the atomic radius of lead is 155.1 pm.

- **9.** Select the correct statement (s):
  - (A) CsCl mainly shows Schottky defect
- (B) ZnS mainly shows Frenkel defect
- (C) NaCl unit cell contain 4Na<sup>+</sup> and 4Cl<sup>-</sup>
- (D) Truncated octahedron have 24 corners.
- **10.** Select the correct statement(s)
  - (A) The ionic crystal of AgBr has Schottky defect.
  - (B) The unit cell having crystal parameters,  $a = b \neq c$ ,  $\alpha = \beta = 90^{\circ}$ ,  $\gamma = 120^{\circ}$  is hexagonal
  - (C) Ionic compounds having Frenkel defect has high  $r^+/r^-$  ratio.
  - (D) The co-ordination number of Na<sup>+</sup> ion in NaCl is 6

#### **ASSERTION / REASON:**

**11. Statement-1**: In diamond, carbon atoms occupy alternate tetrahedral voids in the FCC lattice formed by the carbon atoms.

**Statement-2**: In diamond, packing fraction is more than 74%.

- (A) Statement-1 is true, statement-2 is true and statement-2 is correct explanation for statement-1.
- (B) Statement-1 is true, statement-2 is true and statement-2 is NOT the correct explanation for statement-1.
- (C) Statement-1 is true, statement-2 is false.
- (D) Statement-1 is false, statement-2 is true.
- 12. Statement-1: Due to Frenkel defect, there is no effect on the density of the crystalline solid.

**Statement-2:** In Frenkel defect, no cation or anion leaves the crystal.

- (A) Statement-1 is true, statement-2 is true and statement-2 is correct explanation for statement-1.
- (B) Statement-1 is true, statement-2 is true and statement-2 is NOT the correct explanation for statement-1.
- (C) Statement-1 is true, statement-2 is false.
- (D) Statement-1 is false, statement-2 is true.
- 13. Statement-1: Conductivity of silicon increased by doping it with group 15 element.

**Statement-2:** Doping means introduction of small amount of impurities like P or As into pure silicon crytstal.

- (A) Statement-1 is true, statement-2 is true and statement-2 is correct explanation for statement-1.
- (B) Statement-1 is true, statement-2 is true and statement-2 is NOT the correct explanation for statement-1.
- (C) Statement-1 is true, statement-2 is false.
- (D) Statement-1 is false, statement-2 is true.

#### TABLE TYPE COMPREHENSION:

#### Column-I

#### Column-II

#### Column-III

- (A) NaCl (Rock salt) structure
- (i) Cation FCC Anion - Tetrahedral void
- (I) All tetrahedral voids are occupied

- (B) CsCl structure
- (ii) Anion FCCCation Tetrahedral voids
- (II) All octahedral voids are occupied

- (C) ZnS (zinc blende) structure
- (iii) Anion SC Cation - Cubic voids
- (III) 50 % of tetrahedral voids are occupied

- (D) CaF<sub>2</sub> (fluorite) structure
- (iv) Anion FCC

  Cation Octahedral

  void
- (IV) All octahedral voids are empty
- **14.** Which of the following is correct match?
  - (A) A, i, I
- (B) A, ii, IV
- (C) A, iv, II
- (D) A, iv, IV

- **15.** Which of the following is incorrect match?
  - (A) B, iii, I
- (B) C, ii, III
- (C) D, i, I
- (D) D, i, IV

- **16.** Which of the following is correct match?
  - (A) D, ii, I
- (B) B, iv, IV
- (C) D, iii, I
- (D) C, ii, IV

#### **MATCH THE COLUMN:**

**17.** Match the column

### Column I

Column II

- (A) Tetragonal and Hexagonal
- (P) are two crystal systems
- (B) Cubic and Rhombohedral
- (Q)  $a = b \neq c$
- (C) Monoclinic and Triclinic
- (R)  $a \neq b \neq c$

(D) Cubic and Hexagonal

(S) a = b = c

**18.** Match the column:

#### Column I

Column II

(A) Rock salt structure

(P) Co-ordination number of cation is 4

(B) Zinc Blend structure

(Q)  $\frac{\sqrt{3a}}{4} = r_+ + r_-$ 

(C) Flourite structure

- (R) Co-ordination number of cation and anion are same
- (S) Distance between two nearest anion is  $\frac{a}{\sqrt{2}}$

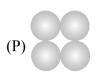


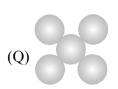
### **MATCHING LIST TYPE:**

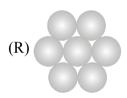
### **19.** Match the column

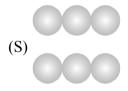
### Column I

(Arrangement of the atoms/ions)









### Code:

P Q R S
(A) 4 3 1 2

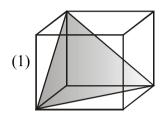
(B) 4 3 2 1

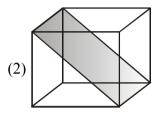
(C) 3 2 1 4

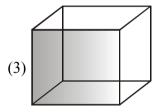
(D) 1 2 4 3

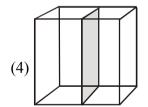
### Column II

(Planes in fcc lattice)









# EXERCISE # J-MAIN

1.	Copper crystallises in fcc with a unit cell edge length of 361pm. What is the radius of copper atom?							
				[AIEEE-2011]				
	(1) 181pm	(2) 128pm	(3) 157pm	(4) 108pm				
2.	The radius of a cal	cium ion is 94 pm and o	of the oxide ion is 146	pm. The possible crystal structure				
	of calcium oxide v	will be :-		[Jee-Main (online)-12]				
	(1) Octahedral	(2) Tetrahedral	(3) Pyramidal	(4) Trigonal				
3.	Ammonium chlor	ide crystallizes in a boo	dy centred cubic lattic	e with edge length of unit cell of				
	390 pm. If the size	e of chloride ion is180	pm, the size of ammo	nium ion would be:				
				[Jee-Main (online)-12]				
	(1) 158 pm	(2) 174 pm	(3) 142 pm	(4) 126 pm				
4.	A solid has 'bcc' s	tructure. If the distance	e of nearest approach l	between two atoms is 1.73 Å, the				
	edge length of the cell is :- [Jee-Main (online)-12]							
	(1) 314.20 pm	(2) 216 pm	(3) 200 pm	(4) 1.41 pm				
<b>5.</b>	Among the follow	ring the incorrect staten	nent is :-	[Jee-Main (online)-12]				
	(1) Density of crys	stals remains unaffecte	d due to Frenkel defec	et				
	(2) In BCC unit cell the void space is 32%							
	(3) Electrical cond	luctivity of semiconduc	ctors and metals increa	ses with increase in temperature				
	(4) Density of cry	(4) Density of crystals decreases due to Schottky defect						
6	Lithium forms bod	ly centred cubic structur	re. The length of the sid	le of its unit cell is 351 pm. Atomic				
	radius of the lithium will be :- [Jee-Main (offline)-12]							
	(1) 152 pm	(2) 75 pm	(3) 300 pm	(4) 240 pm				
7.	In a face centred cubic lattice, atoms of A form the corner points and atoms of B form the face centred							
				ne formula of the ionic compound				
	is			[Jee-Main (online)-13]				
	(1) AB <sub>2</sub>	(2) AB3	(3) AB <sub>4</sub>	(4) A2B5				
8.	Which one of the following statements about packing in solids is <b>incorrect</b> ?							
	(1) Void space in ccp mode of packing is 26% [Jee-Main (online)-13]							
	(2) Coordination number in hcp mode of packing is 12							
	(3) Void space in hcp mode of packing is 32%							
	(4) Coordination number in bcc mode of packing is 8							
9.	An element having an atomic radius of 0.14 nm crystallizes in an fcc unit cell. What is the length							
	of a side of the cell? [Jee-Main (online)-13]							
	(1) 0.96 nm	(2) 0.4 nm	(3) 0.24 nm	(4) 0.56 nm				
10.	· /	\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	* *	3O. Metal M, is present as M <sup>2+</sup> and				
	M <sup>3+</sup> in its oxide. Fraction of the metal which exists as M <sup>3+</sup> would be :- [Jee-Main (offline)-13]							
	(1) 7.01%	(2) 4.08%	(3) 6.05%	(4) 5.08				
11.	The total number	of octahedral void(s) p	er atom present in a cu	ubic close packed structure is :-				
				[Jee-Main (online)-14]				
	(1) 1	(2) 2	(3) 3	(4) 4				

12.	In a monoclinic unit cell, the relation of sides and angles are respectively [Jee-Main (online)-14]						
	(1) $a \neq b \neq c$ and $\alpha \neq \beta \neq \gamma \neq 90^{\circ}$		(2) $a \neq b \neq c$ and $\beta = \gamma = 90^{\circ} \neq \alpha$				
			(4) $a \neq b \neq c$ and $\alpha = \beta = \gamma = 90^{\circ}$				
13.	The appearance of co	olour in solid alkali me	etal halides is generally				
				[Jee-Main (online)-14]			
	` '	` /	. ,	(4) Interstitial position			
14.			<del>-</del>	oms B at the face centred points.			
	If atom B is missing	from one of the face c	1 ,	nula of the ionic compound is:			
	(1) AB	(2) 1 5	=	-2011, Jee-Main (online)-14]			
1 =	$\begin{array}{c} \text{(1) AB}_2 \\ \text{(2) AB}_2 \\ \text{(3) AB}_2 \\ \text{(4) AB}_2 \\ \text{(5) AB}_2 \\ \text{(6) AB}_2 \\ \text{(6) AB}_2 \\ \text{(7) AB}_2 \\ \text{(7) AB}_2 \\ \text{(7) AB}_2 \\ \text{(7) AB}_2 \\ \text{(8) AB}$		$(3) A_5 B_2$				
15.			ice. If 'a' is its eage leng	eth then which of the following			
	expression is correct			[Jee-Main (offline)-14]			
	(1) $r_{Cs^+} + r_{Cl^-} = \frac{\sqrt{3}}{2}a$	$(2) \ r_{Cs^+} + r_{Cl^-} = \sqrt{3}a$	(3) $r_{Cs^+} + r_{Cl^-} = 3a$	$(4) \ r_{Cs^+} + r_{Cl^-} = \frac{3a}{2}$			
16.	Sodium metal crystal	Sodium metal crystallizes in a body centred cubic lattice with a unit cell edge of 4.29Å. The radius					
	of sodium atom is approximately:- [Jee-Main (offline						
	-	(2) 0.93Å	(3) 1 86Å	- ` -			
17.		ing compounds is meta	` '	` '			
17.	(1) $MnO_2$	(2) $TiO_2$	(3) $CrO_2$				
18.	. ,	A metal crystallises in a face centred cubic structure. If the edge length of its unit cell is 'a', the closest					
		vo atoms in metallic cr					
	(1) 2a		(2) $2\sqrt{2}$ a				
	(1) 2a		(2) 2V2 a				
	(3) $\sqrt{2}$ a		(4) $\frac{a}{\sqrt{2}}$				
	$(3) \sqrt{2}a$		(4) $\sqrt{2}$				
19.	Which type of effect 'defect' has the presence of cations in the interstitial sites -						
	(1) Vacancy defect		(2) Frenkel defect	[Jee-Main (offline)-18]			
	(3) Metal deficiency	defect	(4) Schottky defect				
20.	All of the following	[Jee-Main (online)-18]					
	(1) RbCl		(2) CsCl				
	(3) LiCl		(4) NaCl				
21.	Which of the following arrangements shows the schematic alignment of magnetic moments of						
	antiferromagnetic substance?			[Jee-Main (online)-18]			
	$(1) \bigoplus \bigoplus \bigoplus \bigoplus \bigoplus$		$(2) \bigoplus \bigoplus \bigoplus \bigoplus \bigoplus$				
	$(3) \bigoplus \bigoplus \bigoplus$	$\bigoplus$	$(4) \bigoplus \bigoplus \bigoplus$	$\oplus$			

22. An element crystallises in a face-centred cubic (fcc) unit cell with cell edge a. The distance between the centres of two nearest octahedral voids in the crystal lattice is [Jee-Main (online)-2020]

(1)a

(2)  $\sqrt{2}a$  (3)  $\frac{a}{\sqrt{2}}$ 

(4)  $\frac{a}{2}$ 

A diatomic molecule X<sub>2</sub> has a body-centred cubic (bcc) structure with a cell edge of 300 pm. The density 23. of the molecule is  $6.17 \text{ g cm}^{-3}$ . The number of molecules present in 200 g of  $X_2$  is

(Avogadro constant (N<sub>A</sub>) =  $6 \times 10^{23} \text{ mol}^{-1}$ )

[Jee-Main (online)-2020]

 $(1) 8 N_A$ 

 $(2) 40 N_A$ 

 $(3) 4 N_A$ 

(4)  $2 N_{\Delta}$ 

A crystal is made up of metal ions 'M<sub>1</sub>' and 'M<sub>2</sub>' and oxide ions. Oxide ions form a ccp lattice structure. 24. The cation 'M<sub>1</sub>' occupies 50% of octahedral voids and the cation 'M<sub>2</sub>' occupies 12.5% of tetrahedral voids of oxide lattice. The oxidation numbers of  ${}^{t}M_{1}{}^{t}$  and  ${}^{t}M_{2}{}^{t}$  are, respectively :

[Jee-Main (online)-2020]

(1) + 2, +4

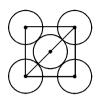
(2) +3, +1

(3) +1, +3

(4) +4, +2

## EXERCISE # J-ADVANCED

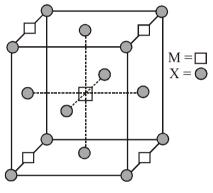
1. The packing effeciency of the two-dimensional square unit cell shown below is [JEE-2010]



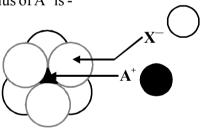
- (A) 39.27%
- (B) 68.02%
- (C) 74.05%
- (D) 78.54%
- 2. The number of hexagonal faces that present in a truncated octahedron is.

[JEE-2011]

3. A compound  $M_p X_q$  has cubic close packing (ccp) arrangement of X. Its unit cell structure is shown below. The empirical formula of the compound is: [JEE-2012]



- (A) MX
- (B) MX,
- $(C) M_2X$
- (D)  $M_5X_{14}$
- 4. The arrangement of  $X^-$  ions around  $A^+$  ion in solid AX is given in the figure (not drawn to scale). If the radius of  $X^-$  is 250 pm, the radius of  $A^+$  is -



- (A) 104 pm
- (B) 125 pm
- (C) 183 pm
- (D) 57 pm
- 5. If the unit cell of a mineral has cubic close packed (ccp) array of oxygen atoms with m fraction of octahedral holes occupied by aluminium ions and n fraction of tetrahedral holes occupied by magnesium ions m and n respectively, are [JEE-2015]
  - (A)  $\frac{1}{2}, \frac{1}{8}$
- (B)  $1, \frac{1}{4}$
- (C)  $\frac{1}{2}, \frac{1}{2}$
- (D)  $\frac{1}{4}, \frac{1}{8}$
- 6. The **CORRECT** statement(s) for cubic close packed (ccp) three dimensional structure is (are)
- (A) The number of the nearest neighbours of an atom present in the topmost layer is 12
  - (B) The efficiency of atom packing is 74%

[JEE-2016]

- (C) The number of octahedral and tetrahedral voids per atom are 1 and 2, respectively
- (D) The unit cell edge length is  $2\sqrt{2}$  times the radius of the atom

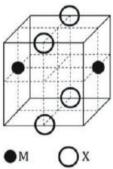
- A crystalline solid of a pure substance has a face-centred cubic structure with a cell edge of 400 pm. If the density of the substance in the crystal is  $8g \text{ cm}^{-3}$ , then the number of atoms present in 256g of the crystal is  $N \times 10^{24}$ . The value of N is
- 8. Consider an ionic solid MX with NaCl structure. Construct a new structure (Z) whose unit cell is constructed from the unit cell of MX following the sequential instructions given below. Neglect the charge balance.

[JEE-2018]

- (i) Remove all the anions (X) except the central one
- (ii) Replace all the face centered cations (M) by anions (X)
- (iii) Remove all the corner cations (M)
- (iv) Replace the central anion (X) with cation (M)

The value of 
$$\left(\frac{\text{number of anions}}{\text{number of cations}}\right)$$
 in Z is\_\_\_\_\_.

9. The cubic unit cell structure of a compound containing cation M and anion X is shown below. When compared to the anion, the cation has smaller ionic radius. Choose the correct statement(s).
[JEE-2020]



- (A) The empirical formula of the compound is MX.
- (B) The cation M and anion X have different coordination geometries.
- (C) The ratio of M-X bond length to the cubic unit cell edge length is 0.866.
- (D) The ratio of the ionic radii of cation M to anion X is 0.414.

### ANSWER KEY

# EXERCISE # S-I

- 1. Ans. (a) 300 pm, (b) 255 pm, (c) 210 pm
- Ans. 5.83 g cm<sup>-3</sup> **3.**
- 5. Ans. (0.9 gm/cm<sup>-3</sup>)
- 7. Ans. (64)
- 9. Ans. (6)
- 11. Ans. (4)
- Ans. (2)  $\frac{\frac{a}{\sqrt{2}} \times \sqrt{2}}{\frac{a}{\sqrt{2}}} = 2$ 13.
- **15. Ans.**(6)
- Ans.346.4 pm **17.**
- Ans.a = 600 pm,  $V = 2.16 \times 10^{-22}$  cm<sup>3</sup> **19.**
- $Ans.6.0 \times 10^{18}$ *21*.
- 23. Ans. 3.0 gm/cm<sup>3</sup>

- 2. Ans. 438 pm, 219 pm
- **Ans.**  $(\sqrt{2}:1)$ 4.
- 6. Ans. (A,B)
- 8. Ans. (12)
- **10.** Ans. A,BC
- **12.** Ans. (0.293)
- **14.** Ans. 4, 6, 8
- **16.** Ans. ZnAl<sub>2</sub>O<sub>4</sub>
- **18.** Ans. 4
- Ans. 1.81Å 20.
- Ans. 12.5% 22.

### EXERCISE # S-II

- 1. Ans. (5)
- **3.** Ans. (i) FCC (ii) 0.116 g/cc

- 2. Ans. 60%, +4
- 4. Ans. (a) 1.143, (b) 1.2

### EXERCISE # O-I

- 1. Ans.(A)
- 4. Ans.(D)
- 7. Ans.(C)
- 10. Ans (D)
- **13.** Ans.(C)
- **16.** Ans.(C)
- **19.** Ans.(A)
- 22.
- Ans (D)
- **25.** Ans.(A)
- 28. Ans.(A)
- 31. Ans.(A)
- 34. Ans.(D)
- **37.** Ans.(C)
- **40.** Ans.(C)

- 2. Ans.(D)
- **5.** Ans.(C)
- 8. Ans.(C)
- 11. Ans (B)
- 14. Ans.(C)
- **17.** Ans.(C)
- **20** Ans (D)
- 23. Ans.(C)
- **26.** Ans.(C)
- 29. Ans.(B)
- **32.** Ans.(D)
- **35.** Ans.(B)
- **38.** Ans.(D)

- **3.** Ans.(A)
- 6. Ans.(D)
- 9. Ans (B)
- **12.** Ans.(B)
- **15.** Ans.(B)
- **18.** Ans.(C)
- 21. Ans (C)
- 24. Ans.(C)
- 27. Ans.(B)
- **30.** Ans.(A)
- 33. Ans.(D)
- **36.** Ans(C)
- **39.** Ans.(B)

### EXERCISE # O-II

1. **Ans.**(C)

- 2. Ans.(D)
- 3. Ans.(C)

4. **Ans.**(A)

5. **Ans.(B)** 

6. **Ans.**(C)

9.

7. **Ans.**(C)

- 8. Ans.(A,C)
- 0. /ms.(c)

Ans.(A,B,C,D)

10. Ans.(A,B,D)

- 11. Ans.(C)
- 12 Ans.(A)

13. Ans.(A)

- 14. Ans.(C)
- 15. Ans.(A)

- 16. Ans.(D)
- 17. Ans.(A)  $\rightarrow$  P, Q; (B)  $\rightarrow$  P,S; (C)  $\rightarrow$  P,R; (D)  $\rightarrow$  P
- 18. Ans.(A)  $\rightarrow$  R,S; (B)  $\rightarrow$  P,Q,R,S; (C)  $\rightarrow$  Q
- 19. **Ans.Ans.(A)**

# EXERCISE # J-MAIN

1. Ans.(2)

2 Ans.(1)

3. Ans.(1)

4. Ans.(3)

5. Ans.(3)

6 Ans.(1)

7. Ans.(3)

8. Ans.(3)

9. Ans.(2)

10. Ans.(2)

- 11. Ans.(1)
- 12. Ans.(2)

13. Ans.(2)

- 13. Ans.(4)
- 15. Ans.(1)

**16.** Ans.(3)

17. Ans.(3)

18 Ans. (4)

19. Ans.(2)

20. Ans.(2)

21. Ans.(4)

22. Ans.(3)

23. Ans.(3)

24. Ans.(1)

# EXERCISE # J-ADVANCED

**1. Ans.(D)** 

2. Ans.(8)

**3. Ans.**(**B**)

4. Ans.(A)

- 5. Ans. (A)
- 6. Ans.(B,C,D)

7. Ans.(2)

8. Ans.(3)

9. Ans.(A,C)

Important Notes

# EXERCISE # S-I

#### **METALLIC CRYSTALS**

#### Cubic crystals

- 1. A closed packed structure of uniform spheres has the edge length of 600 pm. Calculate the radius of sphere, if it exist in  $(\sqrt{2} = 1.4, \sqrt{3} = 1.7)$ 
  - (a) simple cubic lattice
- (b) BCC lattice
- (c) FCC lattice

SS0001

2. Xenon crystallises in the face-centred cubic lattice and the edge length of the unit cell is  $438\sqrt{2}$  pm. What is the nearest neighbour distance and what is the radius of xenon atom?

SS0002

3. The effective radius of the iron atom is  $\sqrt{2}$  Å. It has FCC structure. Calculate its density (Fe = 56 amu, N<sub>A</sub> = 6 × 10<sup>23</sup>)

SS0003

4. Calculate the ratio of densities if same element undergoes fcc as well as simple cubic packing. Assume same atomic radius in both crystals.

SS0004

Potassium has body-centred cubic structure with the nearest neighbour distance  $260\sqrt{3} \text{ pm}$ . Its density would be  $(\frac{1}{(5/2)^2} = 0.036 \text{ , N}_A = 6 \times 10^{23}, \text{ K} = 39)$ 

SS0005

A cubic solid is made up of two elements 'A' and 'B'. Atoms 'B' are at the corners of the cube and 'A' at the body centre. What is the simplest formula of compound?

SS0006

7. An element 'X' crystallizes in bcc. Find volume of unit cell in  $(\mathring{A})^3$ , if atomic radius is  $\sqrt{3}$   $\mathring{A}$ .

SS0007

- 8. A lattice has simple cube unit cell then number of faces which meets at a corner of a cube in this lattice is.

  \$\int \text{SS0008}\$
- **9.** How many next nearest neighbours does potassium have in bcc lattice?

SS0009

#### PACKING IN SOLIDS

**10.** A cubic solid is made by atoms 'A' forming close pack arrangement, 'B' occupying one-fourth of tetrahedral void and C occupying half of the octahedral voids. What is the formula of compound?

SS0011

11. If number of nearest neighbours, next nearest ( $2^{nd}$  nearest) neighbour and next to next nearest ( $3^{rd}$  nearest) neighbours are x, y and z respectively for body centred cubic unit cell, then calculate value of  $\frac{xy}{z}$  is.

SS0012

**12.** In FCC unit cell, what fraction of edge is not covered by atoms?



13. For CABC ABC .... packing, distance between two succesive tetrahedral void is X and distance between two successive octahedral void is y in an unit cell, then  $\frac{y\sqrt{2}}{X}$  is

SS0015

#### IONIC CRYSTALS

**14.** If the radius of Mg<sup>2+</sup> ion, Cs<sup>+</sup> ion, O<sup>2-</sup> ion, S<sup>2-</sup> ion and Cl<sup>-</sup> ion are 0.65 Å, 1.69 Å, 1.40 Å, 1.84 Å, and 1.81 Å respectively, calculate the co-ordination numbers of the cations in the crystals of MgS, MgO and CsCl.

SS0021

**15.** The two ions A<sup>+</sup> and B<sup>-</sup> have radii 88 pm and 200 pm respectively. In the closed packed crystal of compound AB, predict the co-ordination number of A<sup>+</sup>.

SS0022

Spinel is a important class of oxides consisting of two types of metal ions with the oxide ions arranged in CCP pattern. The normal spinel has one-eight of the tetrahedral holes occupied by one type of metal ion and one half of the octahedral hole occupied by another type of metal ion. Such a spinel is formed by  $Zn^{2+}$ ,  $Al^{3+}$  and  $O^{2-}$ , with  $Zn^{2+}$  in the tetrahedral holes. Give the formula of spinel.

SS0023

17. CsCl has bcc unit cell with edge length 400 pm. Calculate the interionic distance in CsCl.

SS0025

18. The density of KBr is 2.38 g cm<sup>-3</sup>. The length of the edge of the unit cell is 700 pm. Find the number of fomula unit of KBr present in the single unit cell.

$$(N_A = 6 \times 10^{23} \text{ mol}^{-1}, \text{At. mass} : K = 39, \text{Br} = 80)$$

SS0026

19. A crystal of lead(II) sulphide has NaCl structure. In this crystal the shortest distance between Pb<sup>+2</sup> ion and S<sup>2-</sup> ion is 300 pm. What is the length of the edge of the unit cell in lead sulphide? Also calculate the unit cell volume.

SS0027

20. If the length of the body diagonal for CsCl which crystallises into a cubic structure with Cl<sup>-</sup> ions at the corners and Cs<sup>+</sup> ions at the centre of the unit cell, is 7 Å and the radius of the Cs<sup>+</sup> ion is 1.69 Å, what is the radius of Cl<sup>-</sup> ion?

SS0028

#### PROBLEMS RELATED WITH DEFECTS IN SOLID

21. If NaCl is dopped with  $10^{-3}$  mol % SrCl<sub>2</sub>, what is the number of cation vacancies per mole of NaCl?  $(N_A = 6 \times 10^{23})$ 

SS0032

22. A non stoichiometric compound  $Fe_7S_8$  consist of iron in both  $Fe^{+2}$  and  $Fe^{+3}$  form and sulphur is present as sulphide ions. Calculate cation vacancies as a percentage of  $Fe^{+2}$  initially present in the ideal crystal.

SS0034

23. The density of ZnS crystal (Zinc blende structure) having 10% Frenkel defect is

[ 
$$r_{z_n^{2+}} = 40\sqrt{3}pm, r_{s_n^{2-}} = 110\sqrt{3}pm, Zn = 65.2, S = 32$$
 ]

### EXERCISE # S-II

1. The density of diamond from the fact that it has face centred cubic structure with two atoms per lattice point and unit cell edge length of 3.6 Å, is 'x' gm / cm<sup>3</sup>, then the value of (1.458x) is  $(N_A = 6 \times 10^{23})$ 

SS0037

2. What is the percent by mass of titanium in rutile, a mineral that contain titanium and oxygen, if structure can be described as a closest packed array of oxide ions, with titanium in one half of the octahedral holes. What is the oxidation number of titanium? (Ti = 48)

SS0039

- 3. The mineral hawleyite, one form of CdS, crystallizes in one of the cubic lattices, with edge length 5.87Å. The density of hawleyite is  $4.63 \text{ g cm}^{-3}$ . (Cd = 112)
  - (i) In which cubic lattice does hawlevite crystallize?
  - (ii) Find the Schottky defect in g cm<sup>-3</sup>.

SS0043

- **4.** KCl crystallizes in the same type of lattice as does NaCl. Given that  $\frac{r_{Na}^{+}}{r_{Cl}^{-}} = 0.5$  and  $\frac{r_{Na}^{+}}{r_{K^{+}}} = 0.7$  Calculate:
  - (a) The ratio of the sides of unit cell for KCl to that for NaCl and
  - (b) The ratio of densities of NaCl to that for KCl.

$$\left( \left( \frac{8}{7} \right)^3 = 1.5, \frac{74.5}{58.5} = 1.25 \right)$$

# EXERCISE # O-I

SINGLE	CORRECT	

(A) 60.4%

(B) 68%

SIIV	GLE CORRECT:				
1.	Which of the following	g are the correct axial dis	stances and axial angles fo	or rhombohedral syst	em?
	(A) $a = b = c$ , $\alpha = \beta =$	_	(B) $a = b \neq c, \alpha = \beta$		
	(C) $a \neq b = c$ , $\alpha = \beta =$	· ·	(D) $a \neq b \neq c, \alpha \neq \beta$	•	
	•	•		·	SS0050
2.	$a \neq b \neq c, \alpha \neq \beta \neq \gamma \neq \beta \neq \beta$	= 90° represents			
	(A) tetragonal system	1	(B) orthorhombic sys	tem	
	(C) monoclinic system		(D) triclinic system		
					SS0051
<b>3.</b>	Diamond belongs to the	ne crystal system :			
	(A) Cubic	(B) triclinic	(C) tetragonal	(D) hexagonal	
					SS0052
4.	A match box exhibits -	-			
	(A) Cubic geometry		(B) Monoclinic geom	etry	
	(C) Tetragonal geomet	try	(D) Orthorhombic ge	ometry	
					SS0053
5.	Which of the following directions?	ng solids substances will	l have same refractive in	dex when measured	in different
	(A) NaCl		(B) Monoclinic sulph	ur	
	(C) Rubber		(D) Graphite		
	(0)110001		( <i>b</i> ) 31 <b>u</b> pini		SS0054
	A	. 11	CA: 4.1 C	1 1D: 41	
6.	-	_	f A ions at the corners of a		
	the faces of the cube.	The empirical formula of	f this compound would be	÷- [A	AIEEE-05]
	$(A)A_2B$	(B)AB	$(C)A_3B$	$(D)AB_3$	
					SS0142
7.	In the body-centred cub	oic unit cell & face centre	d cubic unit cell, the radius	of atom in terms of e	dge lengh(a)
	of the unit cell is respe	ctively:			
	$(A) \frac{a}{a} = a$	(B) $\frac{a}{2\sqrt{2}}, \frac{\sqrt{3}a}{4}$	(C) $\frac{\sqrt{3}a}{4}, \frac{a}{2\sqrt{2}}$	(D) $\frac{\sqrt{3}a}{2}, \frac{a}{2\sqrt{2}}$	
	(A) $\frac{a}{2}$ , $\frac{a}{2\sqrt{2}}$	(B) $\frac{1}{2\sqrt{2}}, \frac{1}{4}$	$(C)$ $\frac{1}{4}$ , $\frac{1}{2\sqrt{2}}$	(D) $\frac{1}{2}$ , $\frac{1}{2\sqrt{2}}$	
					SS0055
8.	Crystal system in which	ch maximum number of	Bravais lattices are possi	hleis	
•	(A) Cubic	(B) Triclinic	(C) Orthorhombic	(D) Rhombohed	ral
	( )	( )	(1) 1 1 1 1 1	( )	SS0056
9.	Number of atoms at s	econd nearest position	from a given atom in a B	CC structure is	
•	(A) 8	(B) 6	(C) 12	(D) 4	
	<b>、</b> /	<b>、</b> /	<b>\</b> /	<b>\</b> /	SS0057
10.	Percentage area of ea	ch face covered by ato	ms in a FCC unit cell is -	_	
•					

(C) 74%

Ε

(D) 78.5%

Solid State

 $(C) X_2 Y$ 

(B) X<sub>2</sub>Y<sub>3</sub>

(D)  $X_3Y_4$ 

**SS0146** 

E

 $(A) X_4 Y_3$ 

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20.	In fcc unit cell small (a = edge length of u	est distance between oct init cell)	tahedral void & tetrahed	dral void is -	
	(A) $\frac{a}{\sqrt{2}}$	(B) $\frac{\sqrt{3} a}{2}$	(C) a	(D) $\frac{\sqrt{3} a}{4}$	
					SS0067
21.	_	rding hexagonal close pa	cking (hcp)		
	(A) packing fraction				
	(B) coordination num				
	(C) ABC ABCtyp	= =	alvoida		
	(D) Containing both	tetrahedral and octahedra	ai voius		SS0068
22	X 1:1 04 04	. 1.	1	. 11	
22.		ving arrangement distanc	e between two nearest ne	eighbours is maximum,	considering
	identical sized atoms	C	(G) (	(D) 1: 11	
	(A) Simple cubic	(B) bcc	(C) fcc	(D) equal in all	000000
					SS0069
23.	How many unit cell	are there in 1 gram cubic	crystal of NaCl?		
	$(A) \frac{4 \times N_A}{58.5}$	$(B) \frac{N_A}{58.5}$	$(C) \frac{N_A}{58.5 \times 4}$	(D) $\frac{N_A}{58.5 \times 8}$	
					SS0070
24.		are present in a cube-sh	-	_	
	(A) $1.28 \times 10^{21}$ unit		(B) $1.71 \times 10^{21}$ un		EEE-03]
	(C) $2.57 \times 10^{21}$ unit	cells	(D) $5.14 \times 10^{21}$ un	it cells	SS0147
25.	The edge length of a	face centred cubic cell	of an ionic substance is	508 pm. If the radius of	of the cation
	is 110 pm, the radiu	s of the anion is :-		[AIE	EEE-10]
	(A) 144 pm	(B) 288 pm	(C) 398 pm	(D) 618 pm	
					SS0148
26.	The coordination nu	mber of cation and anion	in Fluorite CaF <sub>2</sub> and Cs	Cl are respectively	
	(A) 8:4 and 6:3	(B) 6:3 and 4:4	(C) 8:4 and 8:8	(D) 4:2 and 2:4	
					SS0072
27.	A compound XY cry 225 pm, then the rad	ystallizes in 8 : 8 lattice in sof X <sup>+</sup> is	with unit cell edge leng	ht of 480 pm. If the rac	lius of Y <sup>–</sup> is
	(A) 127.5 pm	(B) 190.68 pm	(C) 225 pm	(D) 255 pm	
	-	•	-		SS0073

(A) 54.35 pm

(A) 1 Cs<sup>+</sup> and 1 Cl<sup>-</sup>

28.

(B) 100 pm

(B) 1 Cs<sup>+</sup> and 6 Cl<sup>-</sup>

The mass of a unit cell of CsCl corresponds to

(C) 145.16 pm

(C)  $4 \text{ Cs}^+$  and  $4 \text{ Cl}^-$ 

(D) none of these

(D) 8 Cs<sup>+</sup> and 1 Cl<sup>-</sup>

SS0149

A	LLEN			Solid St	tate 63		
30.	Edge length of M <sup>+</sup> X	K <sup>-</sup> (NaCl structure) is 7.2.	Å. Assuming M <sup>+</sup> – X <sup>-</sup> cont	act along the cell edge, r	adius of X-		
	ion is $(r_{M^+} = 1.6 \text{Å})$	:					
	(A) 2.0 Å	(B) 5.6  Å	(C) $2.8 \text{Å}$	(D) 38 Å			
					SS0150		
31.	NH <sub>4</sub> Cl crystallizes	in CsCl type lattice with	a unit cell edge length of	387 pm. The distance b	etween the		
	oppositively charg	ed ions in the lattice is					
	(A) 335.1 pm	(B) 83.77 pm	(C) 274.46 pm	(D) 137.23 pm			
					SS0077		
32.		$r_{Cl}$ = 181 pm in NaCl (1	rock salt) structure. Wha	t is the shortest distance	e between		
	Na <sup>+</sup> ions? (A) 778.3 pm	(B) 276 pm	(C) 195.7 pm	(D) 390.3 pm			
	r	( ) · · · r	(-) r	( ) 1	SS0078		
			2				
33.	AB crystallises its	elf as NaCl crystal. If r <sub>+</sub>	$r_{-}=\frac{2}{\sqrt{6}}$ and $r_{-}=\sqrt{6}$ , the	edge length of cube is			
	(A) $2\sqrt{3}$	(B) $\frac{4}{\sqrt{3}}$	(C) $\frac{8}{\sqrt{6}}$	(D) $\frac{16}{\sqrt{6}}$			
	$(A)$ $2\sqrt{3}$	(B) $\sqrt{3}$	$(C)$ $\sqrt{6}$	(D) $\sqrt{6}$			
					SS0079		
34.	Which of the follo	owing is the most likely to	o show schottky defect?		550017		
	(A) CaF <sub>2</sub>	(B) ZnS	(C)AgCl	(D) CsCl			
2-	T 1 G 1 11 1	0	1.1		SS0080		
35.	<ul> <li>In the Schottky defect, in AB type ionic solids</li> <li>(A) cations are missing from the lattice sites and occupy the interstitial sites</li> </ul>						
	(B) equal number of cations and anions are missing						
	<ul><li>(C) anions are missing and electrons are present in their place</li><li>(D) equal number of extra cations and electrons are present in the interstitial sites</li></ul>						
	(D) equal number	i of extra cations and elec	cuons are present in the int	ersutiai sites	SS0081		
36.	Choose the corre	ect option.					
			touch each other in fcc ur	it cell because they are	not nearest		
		e each other in fcc lattice		will be 24			
			ther Na <sup>+</sup> in Na <sub>2</sub> O crystal voids in simple cub		e 'a' where		
		of edge of unit cell	1				
	(D) By defects in	n solids, density of solids	either remains constant or	decreases but it can nev			
					SS0082		
37.			and the theoretical density	1s 5.6 / g/cm <sup>-3</sup> . These da	ata indicate		
	that solid AgI has - (A) Schottky defect		(B) Frenkel defect				
	(C) Interstitial impu		(D) Both (A) and (	B)			
	, r			,	SS0083		

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- **38.** Which of the following statement is **CORRECT**?
  - (A) A metal can show only non-stoichiometric defects
  - (B) Schottky defect reduces the density of a solid due to significant increase in volume.
  - (C) Impurity defect always change the density.
  - (D) Solids having F-centres may have metal excess defect due to missing anions.

SS0084

**39.** What type of crystal defect is indicated in the diagram below?

[AIEEE-04]

Na <sup>+</sup>	Cl <sup>-</sup>	$Na^+$	Cl <sup>-</sup>	$Na^+$	Cl <sup>-</sup>
Cl <sup>-</sup>		Cl-	$Na^+$		$Na^+$
$Na^+$	Cl-		Cl-	$Na^+$	Cl <sup>-</sup>
Cl <sup>-</sup>	Na	$^{+}Cl^{-}$	$Na^+$		$Na^+$

(A) Frenkel defect

(B) Schottky defect

(C) Interstitial defect

(D) Frenkel and Schottky defects

SS0151

**40.** Lattice energy of an ionic compound depends upon -

[AIEEE-05]

(A) Size of the ion only

- (B) Charge on the ion only
- (C) Charge on the ion and size of the ion
- (D) Packing of ions only

#### EXERCISE # O-II

#### **SINGLE CORRECT:**

- 1. The only incorrect statement for the packing of identical spheres in two dimension is:
  - (A) For square close packing, coordination number is 4.
  - (B) For hexagonal close packing, coordination number is 6.
  - (C) There is only one void per atom in both, square and hexagonal close packing.
  - (D) Hexagonal close packing is more efficiently packed than square close packing.

SS0085

- 2. Which of the following statements is correct in the rock-salt structure of an ionic compounds?
  - (A) coordination number of cation is four whereas that of anion is six.
  - (B) coordination number of cation is six whereas that of anion is four.
  - (C) coordination number of each cation and anion is four.
  - (D) coordination number of each cation and anion is six.

SS0087

- 3. Which one of the following schemes of ordering closest packed sheets of equal sized spheres do not generate close packed lattice.
  - (A) ABCABC
- (B) ABACABAC
- (C)ABBAABBA
- (D) ABCBCABCBC

SS0064

- 4. Copper metal crystallizes in FCC lattice. Edge length of unit cell is 362 pm. The radius of largest atom that can fit into the voids of copper lattice without disturbing it is
  - (A) 53 pm
- (B) 45 pm
- (C) 93 pm
- (D) 93 pm

SS0065

- 5. Packing fraction in 2-D hexagonal arrangement of identical sphere is
  - (A)  $\frac{\pi}{3\sqrt{2}}$
- (B)  $\frac{\pi}{3\sqrt{3}}$  (C)  $\frac{\pi}{2\sqrt{3}}$
- (D)  $\pi/6$

SS0066

- The density of CaF<sub>2</sub> (fluorite structure) is 3.18 g/cm<sup>3</sup>. The length of the side of the unit cell is 6. (Ca = 40, F = 19)
  - (A) 253 pm
- (B)  $344 \, pm$
- (C) 546 pm
- (D) 273 pm

SS0071

- 7. Choose the correct option.
  - (A) Two adjacent face centre atom doesn't touch each other in fcc unit cell because they are not nearest atom of face each other in fcc lattice
  - (B) Number of nearest Na<sup>+</sup> ions of another Na<sup>+</sup> in Na<sub>2</sub>O crystal will be 24.
  - (C) Minimum distance between two cubical voids in simple cube unit cell lattice will be 'a' where 'a' is length of edge of unit cell
  - (D) By defects in solids, density of solids either remains constant or decreases but it can never increase.

#### **MORE THAN ONE MAY BE CORRECT:**

- Lead metal has a density of  $11.34 \text{ g/cm}^3$  and crystallizes in a face–centred lattice. Choose the correct alternatives (Pb = 208, N<sub>A</sub> =  $6 \times 10^{23}$ )
  - (A) the volume of one unit cell is  $1.22 \times 10^{-22}$  cm<sup>3</sup>.
  - (B) the volume of one unit cell is  $1.22 \times 10^{-19}$  cm<sup>3</sup>.
  - (C) the atomic radius of lead is 175 pm.
  - (D) the atomic radius of lead is 155.1 pm.

SS0090

- **9.** Select the correct statement (s):
  - (A) CsCl mainly shows Schottky defect
- (B) ZnS mainly shows Frenkel defect
- (C) NaCl unit cell contain 4Na<sup>+</sup> and 4Cl<sup>-</sup>
- (D) Truncated octahedron have 24 corners.

SS0092

- 10. Select the correct statement(s) -
  - (A) The ionic crystal of AgBr has Schottky defect.
  - (B) The unit cell having crystal parameters,  $a = b \neq c$ ,  $\alpha = \beta = 90^{\circ}$ ,  $\gamma = 120^{\circ}$  is hexagonal
  - (C) Ionic compounds having Frenkel defect has high  $r^+/r^-$  ratio.
  - (D) The co-ordination number of Na<sup>+</sup> ion in NaCl is 6

SS0093

#### **ASSERTION / REASON:**

**11. Statement-1**: In diamond, carbon atoms occupy alternate tetrahedral voids in the FCC lattice formed by the carbon atoms.

**Statement-2**: In diamond, packing fraction is more than 74%.

- (A) Statement-1 is true, statement-2 is true and statement-2 is correct explanation for statement-1.
- (B) Statement-1 is true, statement-2 is true and statement-2 is NOT the correct explanation for statement-1.
- (C) Statement-1 is true, statement-2 is false.
- (D) Statement-1 is false, statement-2 is true.

SS0097

- 12. Statement-1: Due to Frenkel defect, there is no effect on the density of the crystalline solid.
  - **Statement-2:** In Frenkel defect, no cation or anion leaves the crystal.
  - (A) Statement-1 is true, statement-2 is true and statement-2 is correct explanation for statement-1.
  - (B) Statement-1 is true, statement-2 is true and statement-2 is NOT the correct explanation for statement-1.
  - (C) Statement-1 is true, statement-2 is false.
  - (D) Statement-1 is false, statement-2 is true.

- 13. Statement-1: Conductivity of silicon increased by doping it with group 15 element.
  - **Statement-2:** Doping means introduction of small amount of impurities like P or As into pure silicon crytstal.
  - (A) Statement-1 is true, statement-2 is true and statement-2 is correct explanation for statement-1.
  - (B) Statement-1 is true, statement-2 is true and statement-2 is NOT the correct explanation for statement-1.
  - (C) Statement-1 is true, statement-2 is false.
  - (D) Statement-1 is false, statement-2 is true.

SS0099

#### TABLE TYPE COMPREHENSION:

(A)	Column-I NaCl (Rock salt) structure	(i)	Column-II Cation - FCC Anion - Tetrahedral	(I)	<b>Column-III</b> All tetrahedral voids are occupied
			void		
(B)	CsCl structure	(ii)	Anion - FCC	(II)	All octahedral voids are
			Cation - Tetrahedral		occupied
			voids		
(C)	ZnS (zinc blende)	(iii)	Anion - SC	(III)	50 % of tetrahedral voids
	structure		Cation - Cubic voids		are occupied
(D)	CaF <sub>2</sub> (fluorite)	(iv)	Anion - FCC	(IV)	All octahedral voids are
	structure		Cation - Octahedral		empty
			void		

- 14. Which of the following is correct match?
  - (A) A, i, I
- (B) A, ii, IV
- (C) A, iv, II
- (D) A, iv, IV

SS0106

- **15.** Which of the following is incorrect match?
  - (A) B, iii, I
- (B) C, ii, III
- (C) D, i, I
- (D) D, i, IV

SS0107

- **16.** Which of the following is correct match?
  - (A) D, ii, I
- (B) B, iv, IV
- (C) D, iii, I
- (D) C, ii, IV

### **MATCH THE COLUMN:**

#### **17.** Match the column

#### Column I

- (A) Tetragonal and Hexagonal
- (B) Cubic and Rhombohedral
- (C) Monoclinic and Triclinic
- (D) Cubic and Hexagonal

#### Column II

- (P) are two crystal systems
- (Q)  $a = b \neq c$
- (R)  $a \neq b \neq c$
- (S) a = b = c

SS0109

# **18.** Match the column:

#### Column I

- (A) Rock salt structure
- (B) Zinc Blend structure
- (C) Flourite structure

#### Column II

- (P) Co-ordination number of cation is 4
- (Q)  $\frac{\sqrt{3}a}{4} = r_+ + r_-$
- (R) Co-ordination number of cation and anion are same
- (S) Distance between two nearest anion is  $\frac{a}{\sqrt{2}}$



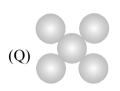
### **MATCHING LIST TYPE:**

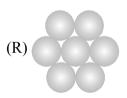
#### **19.** Match the column

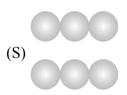
### Column I

(Arrangement of the atoms/ions)









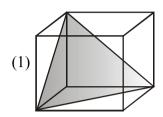
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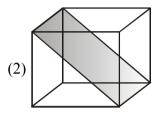
Q P R S(A) 3 2 1 (B) 3 2 4 1 (C) 3 2 1 4 (D) 2 4 3

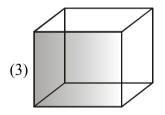
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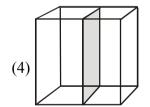
# Column II

(Planes in fcc lattice)









# EXERCISE # J-MAIN

1.	Copper crystallise		edge length of 361pm.	What is the radius of copper atom
	copper on journess	2 11 100 W 101 W 01 00 00 00 00 00 00 00 00 00 00 00 00	ange remgan er e er prim	[AIEEE-2011]
	(1) 181pm	(2) 128pm	(3) 157pm	(4) 108pm
	( ) 1	( ) 1	( ) 1	SS0153
2.	The radius of a cal	cium ion is 94 pm and o	f the oxide ion is 146 r	om. The possible crystal structure o
	calcium oxide will	•	•	[Jee-Main (online)-12]
	(1) Octahedral	(2) Tetrahedral	(3) Pyramidal	(4) Trigonal
				SS0154
3.		ride crystallizes in a bore of chloride ion is180	•	ce with edge length of unit cell onium ion would be:
				[Jee-Main (online)-12]
	(1) 158 pm	(2) 174 pm	(3) 142 pm	(4) 126 pm
				SS0155
4.	A solid has 'bcc' str length of the cell is		f nearest approach be	tween two atoms is 1.73 Å, the edg  [Jee-Main (online)-12]
	(1) 314.20 pm	(2) 216 pm	(3) 200 pm	(4) 1.41 pm
				SS0150
<b>5.</b>	Among the following	ing the incorrect stateme	nt is :-	[Jee-Main (online)-12]
	` '	stals remains unaffecte		ect
	` '	ell the void space is 32		
		-		ases with increase in temperature
	(4) Density of crys	stals decreases due to Sc	chottky defect	CC01 #
	1:4: 6 1 1	. 1 1:	TPL 1 41 C41 : 1	SS0157
6	of the lithium will b	oe:-	-	f its unit cell is 351 pm. Atomic radiu  [Jee-Main (offline)-12]
	(1) 152 pm	(2) 75 pm	(3) 300 pm	(4) 240 pm
				SS0119
7.		ŕ	•	and atoms of B form the face centred the formula of the ionic compound [Jee-Main (online)-13]
	$(1) AB_2$	$(2) AB_3$	$(3) AB_4$	$(4) A_2 B_5$
				SS0120
8.	Which one of the f	following statements about	out packing in solids is	sincorrect?
	(1) Void space in o	ecp mode of packing is	26%	[Jee-Main (online)-13]
	(2) Coordination n	number in hcp mode of p	packing is 12	
	(3) Void space in	hcp mode of packing i	is 32%	

(4) Coordination number in bcc mode of packing is 8

side of the cell?

(2) 0.4 nm

(1) 0.96 nm

9.

[Jee-Main (online)-13]

(4) 0.56 nm

				SS0122
10.	M <sup>3+</sup> in its oxide. Frac	ction of the metal whic	h exists as M <sup>3+</sup> would	Metal M, is present as M <sup>2+</sup> and be :- [Jee-Main (offline)-13]
	(1) 7.01%	(2) 4.08%	(3) 6.05%	(4) 5.08
				SS0123
11.	The total number of o	ctahedral void(s) per at	om present in a cubic cl	ose packed structure is:-
				[Jee-Main (online)-14]
	(1) 1	(2) 2	(3) 3	(4) 4
				SS0124
12.				ely [ <b>Jee-Main (online)-14</b> ]
	(1) $a \neq b \neq c$ and $\alpha =$	$\neq \beta \neq \gamma \neq 90^{\circ}$	(2) $a \neq b \neq c$ and $\beta =$	$= \gamma = 90^{\circ} \neq \alpha$
	(3) $a = b \neq c$ and $\alpha =$	$=\beta=\gamma=90^{\circ}$	(4) $a \neq b \neq c$ and $\alpha =$	$=\beta=\gamma=90^{\circ}$
				SS0125
13.	The appearance of col	lour in solid alkali metal	halides is generally due	e to :
				[Jee-Main (online)-14]
	(1) Frenkel defect	(2) F-centres	(3) Schottky defect	(4) Interstitial position
				SS0126
<b>14.</b>	In a face centred cubic	e lattice atoms A are at th	ne corner points and ato	ms B at the face centred points.
	If atom B is missing	from one of the face co	entred points, the form	ula of the ionic compound is:
			[AIEEE-	2011, Jee-Main (online)-14]
	$(1) AB_2$	$(2) A_2 B_3$	$(3) A_5 B_2$	$(4) A_2 B_5$
				SS0127
<b>15.</b>	CsCl crystallises in bod	ly centred cubic lattice. if	a' is its edge length then v	which of the following expression
	is correct:			[Jee-Main (offline)-14]
	$\sqrt{3}$			3a
	(1) $r_{Cs^+} + r_{Cl^-} = \frac{\sqrt{3}}{2}a$	$(2) \ r_{Cs^+} + r_{Cl^-} = \sqrt{3}a$	(3) $r_{Cs^+} + r_{Cl^-} = 3a$	(4) $r_{Cs^+} + r_{Cl^-} = \frac{3\pi}{2}$
	_			SS0128
16	C - 1:	::_1_1_1_1_1_	-1.:- 1-44::41:4	
16.			abic lattice with a unit co	ell edge of 4.29Å. The radius of
	sodium atom is approx	ximately:-		[Jee-Main (offline)-15]
	(1) 5.72Å	(2) 0.93 Å	(3) 1.86Å	(4) 3.022Å
				SS0129
<b>17.</b>	Which of the following	g compounds is metallic	and ferromagnetic?	[Jee-Main (offline)-16]
	$(1) \mathrm{MnO}_2$	$(2) \operatorname{TiO}_2$	(3) CrO <sub>2</sub>	(4) VO <sub>2</sub>
				SS0130

An element having an atomic radius of 0.14 nm crystallizes in an fcc unit cell. What is the length of a

(3) 0.24 nm

Ε

18.				th of its unit cell is 'a', the clos	
	approach bety	ween two atoms in metal	lic crystal will be :-	[Jee-Main (offline)-1	7]
	(1) 2a	(2) $2\sqrt{2} a$	$(3) \sqrt{2} a$	$(4) \ \frac{a}{\sqrt{2}}$	
				SS01	31
19.	Which type of	f effect 'defect' has the pre	sence of cations in the inters	titial sites -	
	(1) Vacancy d	efect	(2) Frenkel defect	[Jee-Main (offline)-1	8]
	(3) Metal defic	ciency defect	(4) Schottky defect		
				SS01	<b>32</b>
20.		owing share the same crys	[Jee-Main (online)-1	8]	
	(1) RbCl		(2) CsCl		
	(3) LiCl		(4) NaCl	SS01	22
21	W71-:-1 € 41	C-11	_14141114		
21.		following arrangements netic substance?	snows the schematic align	ment of magnetic moments  [Jee-Main (online)-1	
					σJ
	$(1) \bigoplus ($	$\bigcirc \bigcirc \bigcirc \bigcirc \bigcirc$	$(2) \bigoplus \bigoplus \bigoplus \bigoplus$		
	$(3) (\uparrow) (\uparrow) ($	$\bigcirc$	$(4) \bigoplus \bigoplus \bigoplus$	$\bigcirc$	
				SS01	34
22.	An element crys	stallises in a face-centred o	cubic (fcc) unit cell with cell (	edge a. The distance between	the
	•	nearest octahedral voids in	` '	[Jee-Main (online)-202	
	(1) a	$(2) \sqrt{2}a$	$(3) \ \frac{a}{\sqrt{2}}$	(4) $\frac{a}{2}$	
				SS01	58
23.	A diatomic mole	ecule X2 has a body-centre	ed cubic (bcc) structure with a	cell edge of 300 pm. The dens	sitv
		2	ber of molecules present in 2	•	- )

(Avogadro constant (N<sub>A</sub>) =  $6 \times 10^{23}$  mol<sup>-1</sup>)

[Jee-Main (online)-2020]

- $(1) 8 N_A$
- $(2) 40 N_A$   $(3) 4 N_A$
- $(4) 2 N_A$

SS0159

A crystal is made up of metal ions  ${}^{\prime}M_1{}^{\prime}$  and  ${}^{\prime}M_2{}^{\prime}$  and oxide ions. Oxide ions form a ccp lattice structure. 24. The cation  ${\rm 'M_1'}$  occupies 50% of octahedral voids and the cation  ${\rm 'M_2'}$  occupies 12.5% of tetrahedral voids of oxide lattice. The oxidation numbers of  ${}^{t}M_{1}{}^{t}$  and  ${}^{t}M_{2}{}^{t}$  are, respectively :

[Jee-Main (online)-2020]

- (1) +2, +4
- (2) +3, +1
- (3) +1, +3
- (4) +4, +2

# EXERCISE # J-ADVANCED

1. The packing effeciency of the two-dimensional square unit cell shown below is [JEE-2010]



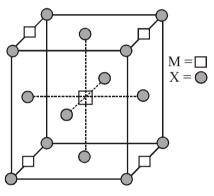
- (A) 39.27%
- (B) 68.02%
- (C) 74.05%
- (D) 78.54%

SS0161

**2.** The number of hexagonal faces that present in a truncated octahedron is.

[JEE-2011] SS0135

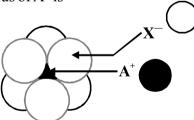
3. A compound  $M_pX_q$  has cubic close packing (ccp) arrangement of X. Its unit cell structure is shown below. The empirical formula of the compound is: [JEE-2012]



- (A) MX
- $(B) MX_2$
- (C) M<sub>2</sub>X
- (D)  $M_5X_{14}$

SS0136

The arrangement of  $X^-$  ions around  $A^+$  ion in solid AX is given in the figure (not drawn to scale). If the radius of  $X^-$  is 250 pm, the radius of  $A^+$  is -



- (A) 104 pm
- (B) 125 pm
- (C) 183 pm
- (D) 57 pm

SS0137

- 5. If the unit cell of a mineral has cubic close packed (ccp) array of oxygen atoms with m fraction of octahedral holes occupied by aluminium ions and n fraction of tetrahedral holes occupied by magnesium ions m and n respectively, are [JEE-2015]
  - (A)  $\frac{1}{2}, \frac{1}{8}$
- (B)  $1, \frac{1}{4}$
- (C)  $\frac{1}{2}, \frac{1}{2}$
- (D)  $\frac{1}{4}, \frac{1}{8}$

SS0138

E

- (A) The number of the nearest neighbours of an atom present in the topmost layer is 12
- (B) The efficiency of atom packing is 74%

[JEE-2016]

- (C) The number of octahedral and tetrahedral voids per atom are 1 and 2, respectively
- (D) The unit cell edge length is  $2\sqrt{2}$  times the radius of the atom

SS0139

A crystalline solid of a pure substance has a face-centred cubic structure with a cell edge of 400 pm. If the density of the substance in the crystal is  $8g \text{ cm}^{-3}$ , then the number of atoms present in 256g of the crystal is  $N \times 10^{24}$ . The value of N is

SS0140

8. Consider an ionic solid MX with NaCl structure. Construct a new structure (Z) whose unit cell is constructed from the unit cell of MX following the sequential instructions given below. Neglect the charge balance.

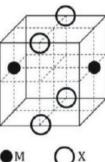
[JEE-2018]

- (i) Remove all the anions (X) except the central one
- (ii) Replace all the face centered cations (M) by anions (X)
- (iii) Remove all the corner cations (M)
- (iv) Replace the central anion (X) with cation (M)

The value of 
$$\left(\frac{\text{number of anions}}{\text{number of cations}}\right)$$
 in Z is\_\_\_\_\_.

SS0141

9. The cubic unit cell structure of a compound containing cation M and anion X is shown below. When compared to the anion, the cation has smaller ionic radius. Choose the correct statement(s).
[JEE-2020]



- (A) The empirical formula of the compound is MX.
- (B) The cation M and anion X have different coordination geometries.
- (C) The ratio of M-X bond length to the cubic unit cell edge length is 0.866.
- (D) The ratio of the ionic radii of cation M to anion X is 0.414.

### ANSWER KEY

### EXERCISE # S-I

- 1. Ans. (a) 300 pm, (b) 255 pm, (c) 210 pm
- Ans. 5.83 g cm<sup>-3</sup> **3.**
- 5. Ans. (0.9 gm/cm<sup>-3</sup>)
- 7. Ans. (64)
- 9. Ans. (6)
- 11. Ans. (4)
- Ans. (2)  $\frac{\frac{a}{\sqrt{2}} \times \sqrt{2}}{\frac{a}{\sqrt{2}}} = 2$ 13.
- **15. Ans.**(6)
- Ans.346.4 pm **17.**
- Ans.a = 600 pm,  $V = 2.16 \times 10^{-22}$  cm<sup>3</sup> **19.**
- $Ans.6.0 \times 10^{18}$ *21*.
- 23. Ans. 3.0 gm/cm<sup>3</sup>

- 2. Ans. 438 pm, 219 pm
- **Ans.**  $(\sqrt{2}:1)$ 4.
- 6. Ans. (A,B)
- 8. Ans. (12)
- **10.** Ans. A,BC
- **12.** Ans. (0.293)
- **14.** Ans. 4, 6, 8
- **16.** Ans. ZnAl<sub>2</sub>O<sub>4</sub>
- **18.** Ans. 4
- Ans. 1.81Å 20.
- Ans. 12.5% 22.

### EXERCISE # S-II

- 1. Ans. (5)
- **3.** Ans. (i) FCC (ii) 0.116 g/cc

- 2. Ans. 60%, +4
- 4. Ans. (a) 1.143, (b) 1.2

### EXERCISE # O-I

- 1. Ans.(A)
- 4. Ans.(D)
- 7. Ans.(C)
- 10. Ans (D)
- **13.** Ans.(C)
- **16.** Ans.(C)
- **19.** Ans.(A)
- 22. Ans (D)
- **25.** Ans.(A)
- 28. Ans.(A)
- 31. Ans.(A)
- 34. Ans.(D)
- **37.** Ans.(C)
- **40.** Ans.(C)

- 2. Ans.(D)
- **5.** Ans.(C)
- 8.
- Ans.(C)
- 11. Ans (B)
- 14. Ans.(C)
- **17.**
- Ans.(C)
- **20** Ans (D) 23.
- **26.** Ans.(C)

Ans.(C)

- 29. Ans.(B)
- **32.** Ans.(D)
- **35.** Ans.(B)
- **38.** Ans.(D)

- **3.** Ans.(A)
- 6. Ans.(D)
- 9. Ans (B)
- **12.** Ans.(B)
- **15.** Ans.(B)
- **18.** Ans.(C)
- 21. Ans (C)
- 24. Ans.(C)
- 27. Ans.(B)
- **30.** Ans.(A)
- 33. Ans.(D)
- **36.** Ans(C)
- **39.** Ans.(B)

### EXERCISE # O-II

1. **Ans.**(C)

- 2. Ans.(D)
- 3. Ans.(C)

4. Ans.(A)

5. **Ans.(B)** 

6. **Ans.**(C)

7. Ans.(C)

- 8. **Ans.**(**A,C**)
- 9. Ans.(A,B,C,D)

10. Ans.(A,B,D)

- 11. Ans.(C)
- 12 Ans.(A)

13. Ans.(A)

- 14. Ans.(C)
- 15. Ans.(A)

- 16. Ans.(D)
- 17. Ans.(A)  $\rightarrow$  P, Q; (B)  $\rightarrow$  P,S; (C)  $\rightarrow$  P,R; (D)  $\rightarrow$  P
- 18. Ans.(A)  $\rightarrow$  R,S; (B)  $\rightarrow$  P,Q,R,S; (C)  $\rightarrow$  Q
- 19. **Ans.Ans.(A)**

## EXERCISE # J-MAIN

1. Ans.(2)

2 Ans.(1)

3. Ans.(1)

4. Ans.(3)

- 5. Ans.(3)
- 6 Ans.(1)

7. Ans.(3)

8. Ans.(3)

9. Ans.(2)

10. Ans.(2)

- 11. Ans.(1)
- 12. Ans.(2)

13. Ans.(2)

13. Ans.(4)

15. Ans.(1)

16. Ans.(3)

17. Ans.(3)

18 Ans. (4)

19. Ans.(2)

20. Ans.(2)

21. Ans.(4)

22. Ans.(3)

23. Ans.(3)

24. Ans.(1)

# EXERCISE # J-ADVANCED

1. **Ans.(D)** 

2. Ans.(8)

 $3. \quad Ans.(B)$ 

4. Ans.(A)

- 5. Ans. (A)
- 6. Ans.(B,C,D)

7. Ans.(2)

8. Ans.(3)

9. Ans.(A,C)

Important Notes